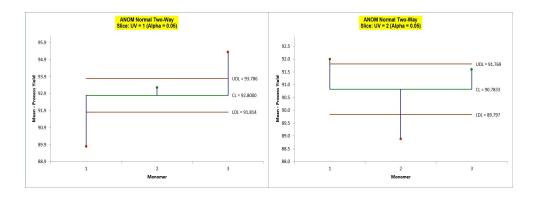


Lean Six Sigma Statistical Tools, Templates & Monte Carlo Simulation in Excel

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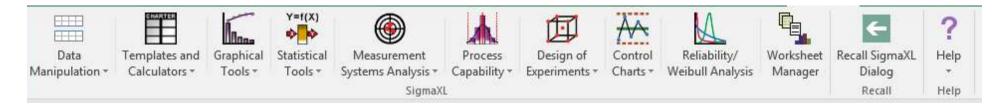


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### **Taguchi Templates:**

- Two Level L4, L8, L12, L16 and L18
- Three Level L9
- Two and Three Level L18
- Easy to use Templates



### **Taguchi Templates:**

- Charts are created automatically:
  - Pareto of Effects/Deltas for Means, StDevs and Signalto-Noise Ratios
  - Pareto of ANOVA SS % Contribution for Means, StDevs and Signal-to-Noise Ratios
  - Overlay Plot of Main Effects for Means, StDevs and Signal-to-Noise Ratios
  - Interaction Plots for Means, StDevs and Signal-to-Noise Ratios (if applicable)



#### Taguchi Template Example – Three Factor L8 Robust Cake

#### Three-Factor, Taguchi L8 Orthogonal Array

Title:	Robust Cake Experiment adapted from Video "Designing Industrial Experiments", Box, Bisgaard, Fung
Date:	
Name of Experimenter:	
Response:	Taste Score (Scale 1-7 where 1 is "awful" and 7 is "delicious"); Outer Array Reps have different Cooking Time and Temp Conditions

Signal-to-Noise Ratio: SN: Larger is Better Target: 1

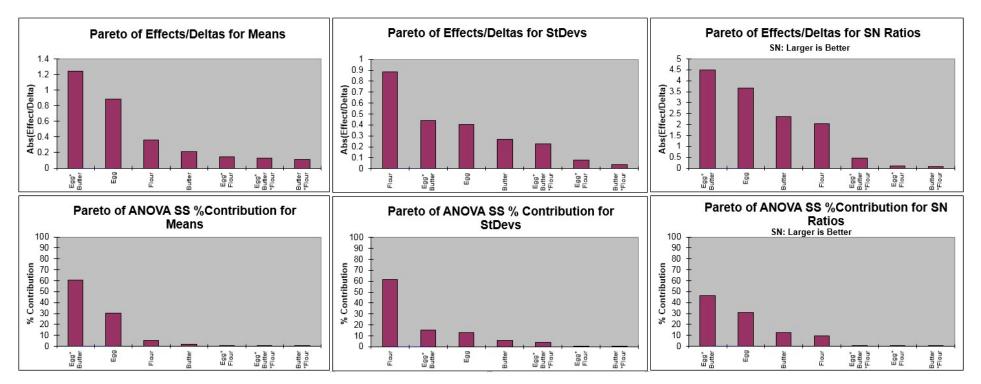
Factor	Factor Name	Low	High
A	Egg	1	2
В	Butter	1	2
С	Flour	1	2

#### Predicted Output for Y:

Factor Name	Enter Actual Factor Setting - uncoded	Factor setting coded	Ŷ	Ŝ	SN: Larger is Better
Egg	2	2	5.9	0.681909085	15.27864445
Butter	1	1			
Flour	2	2			

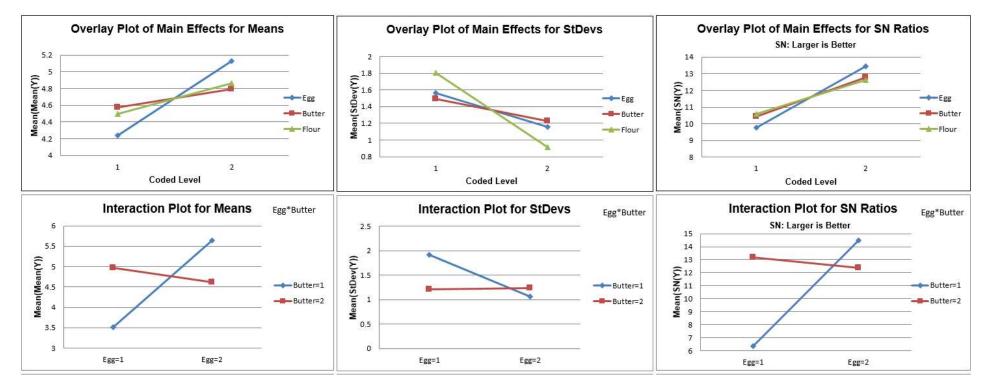


#### Taguchi Template Example – Three Factor L8 Robust Cake





#### Taguchi Template Example – Three Factor L8 Robust Cake

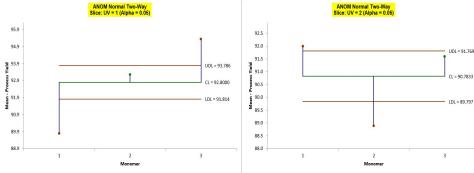




SigmaXL has added some exciting, new and unique features that make multiple comparisons easy:

## Analysis of Means (ANOM) Charts

- Normal, Binomial Proportions and Poisson Rates
  - One-Way
  - Two-Way
    - Main Effects
    - Slice Charts



- Yellow highlight recommendation
- Nonparametric Transformed Ranks
- Variances & Levene Robust Variances
- Supports balanced and unbalanced data



### Multiple Comparisons (a.k.a. Post-Hoc)

- One-Way ANOVA
- Welch ANOVA (Assume Unequal Variance)
- Bartlett & Levene Equal Variance
- Easy to read probabilities in matrix format with significant values highlighted in red

Pairwise Mean Difference (row - column)	1	2	3
1	0	-0.8117	-0.2476
2		0	0.5641
3			0
Tukey Probabilities	1	2	3
1		0.0000	0.3777
2			0.0044
2			

 Appropriate ANOM chart available as a graphical option



#### **Chi-Square Tests & Table Associations**

- Adjusted Residuals (significant values highlighted in red)
- Cell's Contribution to Chi-Square
- Additional Chi-Square Tests
- Tests and Measures of Association for Nominal & Ordinal Categories



#### **Descriptive Statistics**

- Percentile Report and Percentile Ranges
- Percentile Confidence and Tolerance Intervals
- Additional Descriptive Statistics
- Additional Normality Tests
- Outlier and Randomness Tests



### **Templates and Calculators**

- 1 Sample Z test and Confidence Interval for Mean
- Normal Exact Tolerance Intervals
- Equivalence Tests: 1 & 2 Sample Means, 2 Proportions, 2 Poisson Rates
- Type 1 Gage Study, Gage Bias & Linearity Study



# Analysis of Means (ANOM) Charts

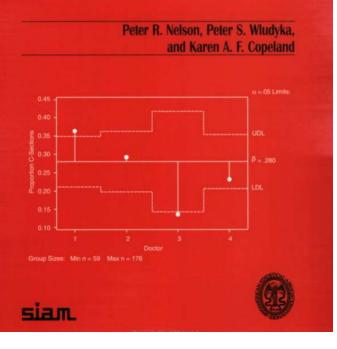
- A statistical procedure for troubleshooting industrial processes and analyzing the results of experimental designs with factors at fixed levels.
- It provides a graphical display of data. Ellis R. Ott developed the procedure in 1967 because he observed that nonstatisticians had difficulty understanding analysis of variance.
- Analysis of means is easier for quality practitioners to use because it is (like) an extension of the control chart.



# **Analysis of Means (ANOM) Charts**

#### The Analysis of Means

A Graphical Method for Comparing Means, Rates, and Proportions



From the Preface:

- The goal of statistical data analysis is to use data to gain and communicate knowledge about processes and phenomena. Comparing means is often part of an analysis, for data arising in both experimental and observational studies.
- The analysis of means (ANOM) is an alternative procedure (to ANOVA) for comparing means.
- ANOM has the advantages of being much more intuitive and providing an easily understood graphical result, which clearly indicates any means that are different (from the overall mean) and allows for easy assessment of practical as well as statistical significance.
- The graphical result is easy for nonstatisticians to understand and offers a clear advantage over ANOVA in that it sheds light on the nature of the differences among the populations.



# **Analysis of Means (ANOM) Charts**

#### The Analysis of Means

A Graphical Method for Comparing Means, Rates, and Proportions



One-Way Balanced\* Normal:

UDL = 
$$\overline{y}_{\bullet} + h(\alpha; I, N - I)\sqrt{MS_e}\sqrt{\frac{I-1}{N}}$$
  
LDL =  $\overline{y}_{\bullet} - h(\alpha; I, N - I)\sqrt{MS_e}\sqrt{\frac{I-1}{N}}$ 

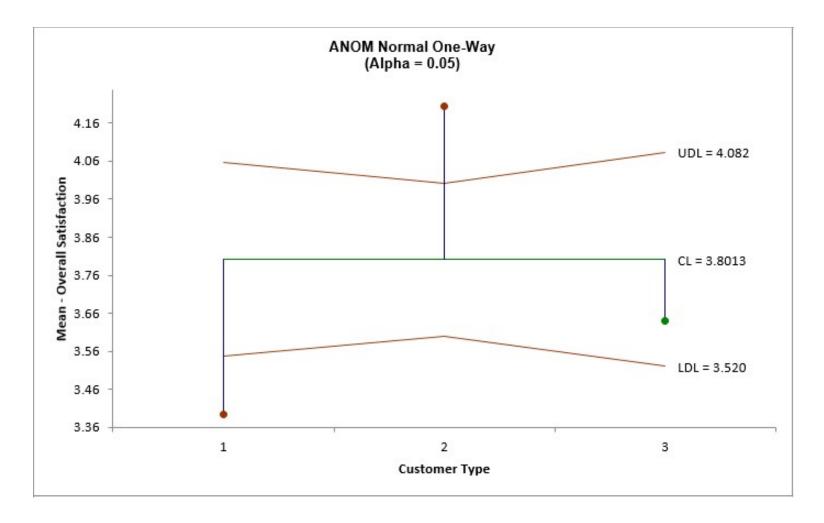
 $\bar{y}_{..}$  = Overall mean h = Critical value from multivariate t distribution – SigmaXL uses table exact critical values (Table B.1) N = Sample size l = Number of levels

 $\sqrt{MS_e}$  SQRT(Mean Square Error) = pooled standard deviation.

\* Unbalanced uses critical values from studentized maximum modulus (SMM) distribution. SigmaXL uses table exact critical values (Table B.2). An adjustment is also made for varying sample size that results in varying decision limit values.



### Example: ANOM Normal One-Way Overall Satisfaction by Customer Type



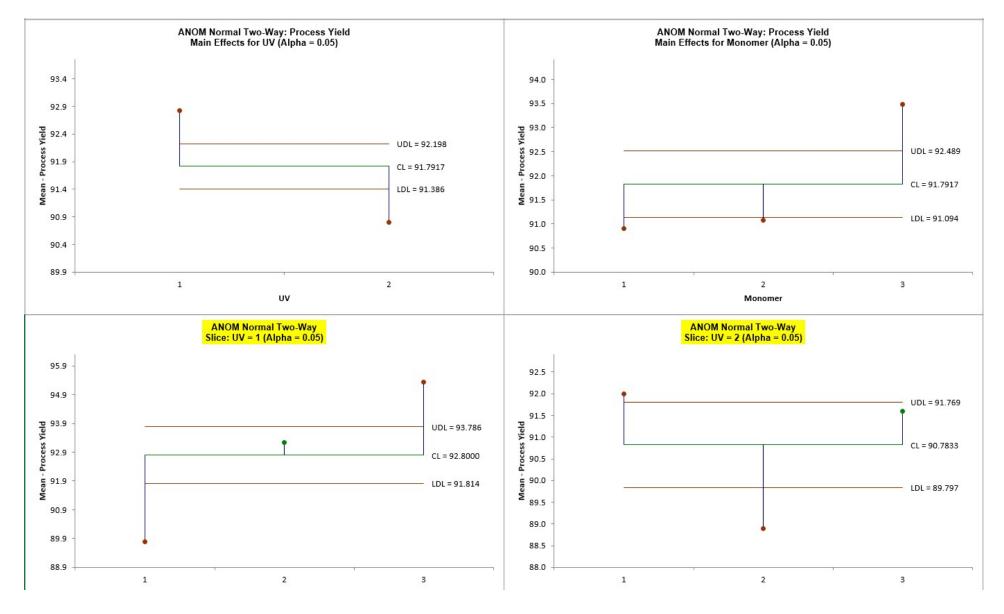


## ANOM Normal Two-Way with Main Effects and Slice Charts

- Main Effects for Two-Way ANOM are similar to One-Way but the mean square error (MSE) is derived from the ANOVA.
- Slice Charts are a modified ANOM chart developed by Dr. Peter Wludyka that enables one to easily interpret the effects in the presence of an interaction (Wludyka 2013, 2015).
  - The basic idea is to compare the levels of one factor for each level of the other factor
  - MSE is still derived from the Two-Way ANOVA
- Yellow highlight automatically recommends Main Effects (if interaction is not significant) or Slice Chart (if interaction is significant). Interaction P-Value is determined from ANOVA
- Option to specify correction to alpha for multiple chart familywise error rate
  - Bonferroni alpha' = alpha/m; m = number of charts

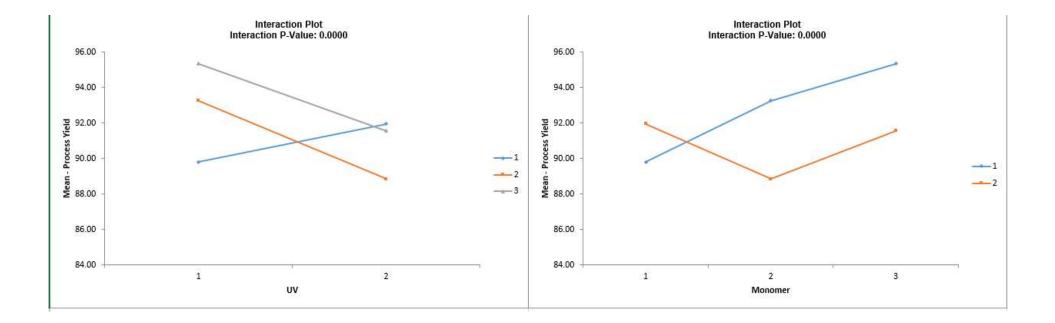


#### "The Analysis of Means" Example 5.3 Process Yield Experiment (used with author permission): Normal Two-Way Main Effects & Slice Charts





"The Analysis of Means" Example 5.3 Process Yield Experiment (used with author permission): Normal Two-Way Interaction Plots





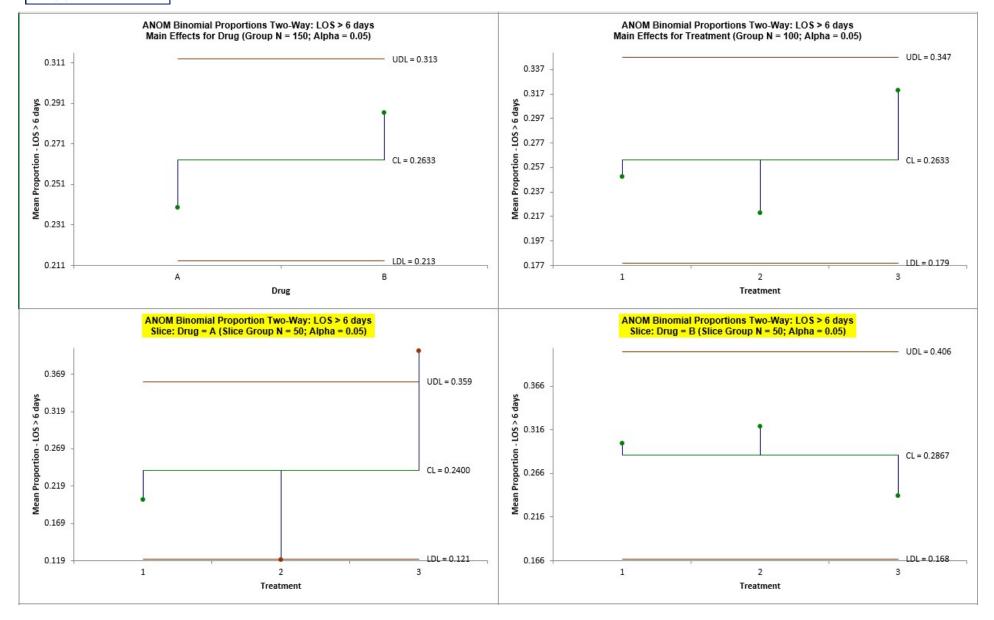
### ANOM Binomial Proportions and Poisson Rates Two-Way with Main Effects and Slice Charts

- In collaboration, Peter Wludyka and John Noguera of SigmaXL extended the Slice Charts to Binomial and Poisson (Wludyka and Noguera 2016).
  - As with Normal, the basic idea is to compare the levels of one factor for each level of the other factor
  - MSE is derived from the whole model
- Yellow highlight automatically recommends Main Effects (if interaction is not significant) or Slice Chart (if interaction is significant).
- Interaction P-Value is automatically determined from Logistic regression for Binomial Proportions and Poisson regression for Poisson Rates.
- Assumes a normal approximation to Binomial or Poisson, so a warning is given if np, nq, or nu <= 5.</li>



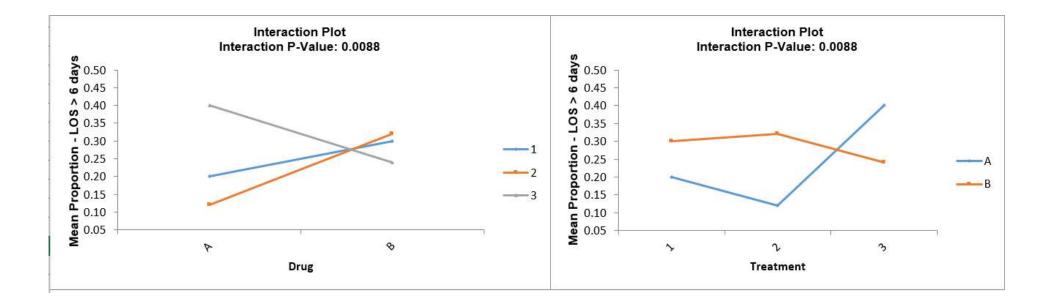
# "The Analysis of Means" Example 5.15 Length of Stay Data (used with author permission):

**Binomial Proportions Two-Way Main Effects & Slice Charts** 



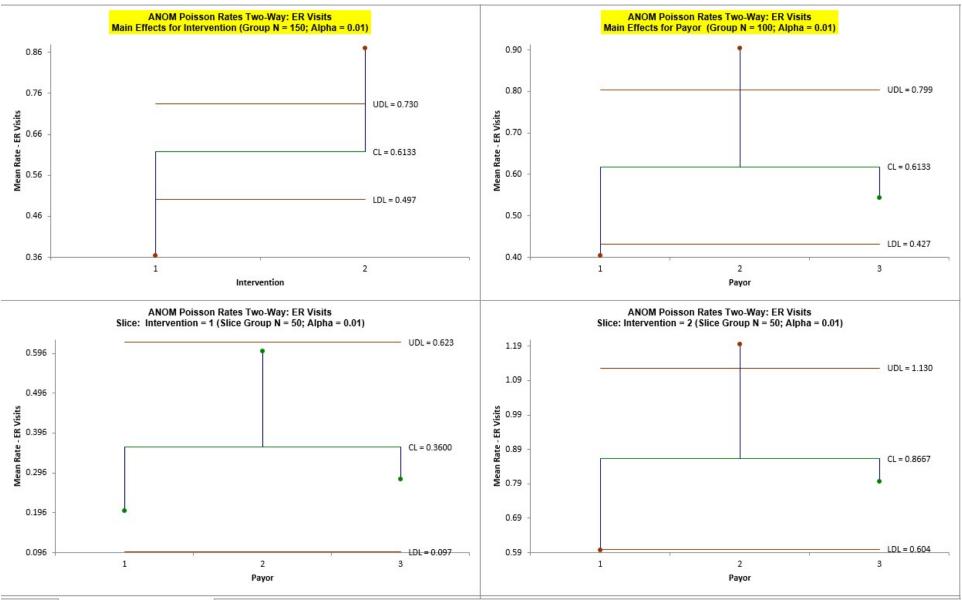


#### "The Analysis of Means" Example 5.15 Length of Stay Data (used with author permission): Binomial Proportions Two-Way Interaction Plots



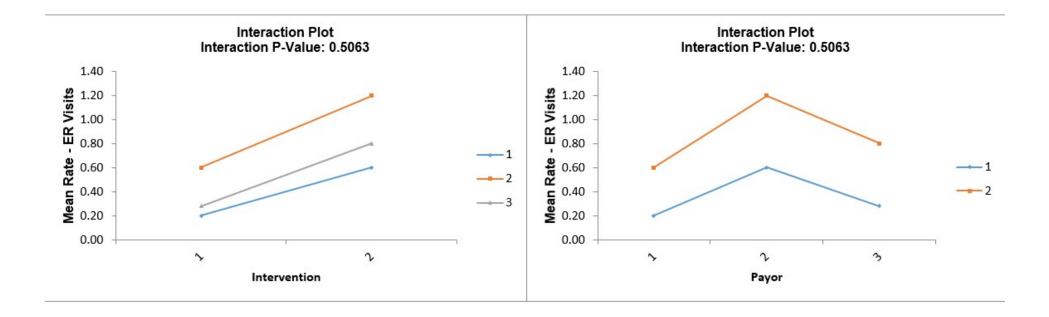


#### "The Analysis of Means" Example 5.16 Emergency Room Visits (used with author permission): Poisson Rates Two-Way Main Effects & Slice Charts





#### "The Analysis of Means" Example 5.16 Emergency Room Visits (used with author permission): Poisson Rates Two-Way Interaction Plots





### **One-Way ANOVA**

- Fisher
  - Also known as Fisher's Least Significant Difference (LSD)
  - Pairwise 2 sample t-tests with pooled standard deviation
  - Does not correct for family wise error rate, so should only be used for k = 3 means and in the restricted case where the ANOVA pvalue is < alpha (this is also known as Protected Fisher LSD). For k = 3 means, Protected Fisher LSD is more powerful than Tukey.

#### • Tukey

 Similar to LSD, uses pairwise tests with pooled standard deviation, but is a studentized range statistic that corrects for family-wise error rate. Recommended for k > 3.



#### **Example of Fisher and Tukey Probabilities for Overall Satisfaction by Customer Type**

Pairwise Mean Difference (row - column)	1	2	3
1	0	-0.8117	-0.2476
2		0	0.5641
3			0
Fisher Pairwise Probabilities	1	2	3
1		0.0000	0.1840
2			0.0016
3			

Pairwise Mean Difference (row - column)	1	2	3
1	0	-0.8117	-0.2476
2		0	0.5641
3			0
Tukey Probabilities	1	2	3
1		0.0000	0.3777
2			0.0044
3			

26



### **One-Way ANOVA**

- Dunnett with Control
  - If one of the groups are a control reference group, Dunnett with Control is more powerful than Tukey because it is doing fewer pairwise comparisons (only considers those pairwise against the control group).
  - Uses pooled standard deviation and the multivariate t distribution that corrects for family-wise error rate.
- Option: Display ANOM Normal One-Way Chart



### Welch ANOVA (Assume Unequal Variance)

#### • Welch Pairwise

- Pairwise 2 sample t-tests with unpooled standard deviation and weighted degrees of freedom (2 sample t-test for unequal variance)
- Does not correct for family wise error rate, so should only be used for k = 3 means and in the restricted case where the Welch ANOVA p-value is < alpha.</li>

#### • Games-Howell

- Similar to Welch Pairwise, uses unpooled standard deviation and weighted degrees of freedom, but is a studentized range statistic that corrects for family-wise error rate. Recommended for k > 3.
- It is an extension of the Tukey test for unequal variance.
- ANOM Chart option is not available for Welch ANOVA as<sub>28</sub> this requires two-stage sampling.



### **Bartlett Equal Variance**

- F-Test
  - Pairwise 2 sample F-tests
  - Does not correct for family wise error rate, so should only be used for k = 3 groups and in the restricted case where the Bartlett pvalue is < alpha.</li>
- F-Test with Bonferroni Correction
  - Pairwise 2 sample F-tests with Bonferroni correction
  - Recommended for k > 3
  - Bonferroni p-value' = p-value \* m
    - m = number of pairwise comparisons k(k-1)/2
- Option: Display ANOM Variances Chart



### Levene (Robust) Equal Variance

- Levene
  - Pairwise 2 sample Levene tests
  - Does not correct for family wise error rate, so should only be used for k = 3 groups and in the restricted case where the Levene pvalue is < alpha.</li>
- Tukey ADM (Absolute Deviations from Median)
  - Application of Tukey on ADM (Absolute Deviations from Median)
  - Recommended for k > 3
  - This post-hoc test is unique to SigmaXL, inspired by the method used in ANOM Levene Variances.
- Option: Display ANOM Levene Robust Variances Chart



## Chi-Square Tests & Table Associations

- Improved dialog labels for stacked data (Rows, Cols, Frequency)
- Adjusted Residuals
  - Red font highlight denotes significant cell residual value
  - Bold red highlight denotes significant cell residual value with Bonferroni adjustment
  - Note: red highlight is only active if Chi-Square P-Value is significant
- Cell's Contribution to Chi-Square



# Chi-Square Tests & Table Associations (Optional)

- Additional Chi-Square Tests
  - Likelihood Ratio
  - McNemar-Bowker Symmetry (Square Table)
- Measures of Association for Nominal Categories
  - Pearson's Phi
    - In a 2x2 table, this is equivalent to Pearson's correlation coefficient
    - Cohen (1977) gives the ROT for general effect sizes: 0.1 = "Small"; 0.3 = "Medium"; 0.5 = "Large"
  - Cramer's V
    - An extension of Phi for larger tables
  - Contingency Coefficient
  - Cohen's Kappa (Agreement Square Table)



## Chi-Square Tests & Table Associations (Optional)

- Measures of Association for Nominal Categories
  - Goodman-Kruskal Lambda (Cols & Rows Dependent, Symmetric)
  - Goodman-Kruskal Tau (Cols & Rows Dependent)
  - Theil's Uncertainty (Cols & Rows Dependent, Symmetric)



# Chi-Square Tests & Table Associations (Optional)

- Tests of Association for Ordinal Categories
  - Concordant Discordant
  - Spearman Rank Correlation
- Measures of Association for Ordinal Categories
  - Spearman Rank Correlation
  - Kendall's Tau-B (Square Table)
  - Kendall-Stuart Tau-C (Rectangular Table)
  - Goodman-Kruskal Gamma
  - Somers' D (Cols & Rows Dependent, Symmetric)



#### Chi-Square Tests & Table Associations Nominal Example: Supplier (Cols) & Pass/Fail/Marginal (Rows)

Chi-Square 2 Way Table Statistics			
Observed Counts	Supplier A	Supplier B	Supplier C
Pass	160	140	150
Fail	20	30	36
Marginal	20	30	14
Expected Counts	Supplier A	Supplier B	Supplier C
Pass	150	150	150
Fail	28.667	28.667	28.667
Marginal	21.333	21.333	21.333
Std. Residuals	Supplier A	Supplier B	Supplier C
Pass	0.816497	-0.816497	0
Fail	-1.619	0.249029	1.370
Marginal	-0.288675	1.876	-1.588
Adjusted Residuals	Supplier A	Supplier B	Supplier C
Pass	2	-2	0
Fail	-2.14191972	0.329526111	1.812393613
Marginal	-0.374066	2.431429007	-2.05736301
Cell's Contribution to Chi-Square	Supplier A	Supplier B	Supplier C
Pass	0.66666667	0.666666667	0
Fail	2.62015504	0.062015504	1.875968992
Marginal	0.08333333	3.520833333	2 520833333



#### Chi-Square Tests & Table Associations Nominal Example: Supplier (Cols) & Pass/Fail/Marginal (Rows)

Chi-Square	12.016			
DF	4			
P-Value	0.0172			
Additional Chi-Square Tests				
Test	Chi-Square	DF	P-Value	
Likelihood Ratio	12.1425	4	0.0163	
McNemar-Bowker Symmetry (Square Table)	189.9572	3	0.0000	
Measures of Association for Nominal Categories				
Measure	Value	Std. Error	95% Lower Bound	95% Upper Bound
Pearson's Phi	0.1415			
Cramer's V	0.1001			
Contingency Coefficient	0.1401			
Cohen's Kappa (Agreement - Square Table)	0.0100	0.0211	-0.0314	0.0514
Goodman-Kruskal Lambda (Cols Dependent)	0.0650	0.0249	0.0162	0.1138
Goodman-Kruskal Lambda (Rows Dependent)	0.0000	0.0000	0.0000	0.0000
Goodman-Kruskal Lambda (Symmetric)	0.0473	0.0181	0.0118	0.0827
Goodman-Kruskal Tau (Cols Dependent)	0.0100	0.0057	0.0000	0.0211
Goodman-Kruskal Tau (Rows Dependent)	0.0095	0.0058	0.0000	0.0209
Theil's Uncertainty (Cols Dependent)	0.0092	0.0052	-0.0010	0.0194
Theil's Uncertainty (Rows Dependent)	0.0138	0.0078	-0.0015	0.0291
Theil's Uncertainty (Symmetric)	0.0110	0.0062	-0.0012	0.0233



#### Chi-Square Tests & Table Associations Ordinal Example: Satisfaction (Cols) & Salary (Rows)

Observed Counts	Very Dissatisfied	Somewhat Dissatisfied	Somewhat Satisfied	Very Satisfied
< 20K	5	6	19	12
20-30K	5	7	20	14
30-40K	3	12	28	24
> 40K	1	2	18	26
Expected Counts	Very Dissatisfied	Somewhat Dissatisfied	Somewhat Satisfied	Very Satisfied
< 20K	2.911	5.614	17.673	15.802
20-30K	3.188	6.149	19.356	17.307
30-40K	4.644	8.955	28.193	25.208
> 40K	3.257	6.282	19.777	17.683
Std. Residuals	Very Dissatisfied	Somewhat Dissatisfied	Somewhat Satisfied	Very Satisfied
< 20K	1.224	0.162972	0.315591	-0.956432
20-30K	1.014757961	0.343393	0.146278	-0.794905
30-40K	-0.762713	1.017372859	-0.036361522	-0.240586
> 40K	-1.251	-1.708	-0.399632	1.978
Adjusted Residuals	Very Dissatisfied	Somewhat Dissatisfied	Somewhat Satisfied	Very Satisfied
< 20K	1.426134732	0.196736411	0.465932976	-1.360693153
20-30K	1.196940639	0.419818923	0.218713418	-1.145298952
30-40K	-0.967089216	1.33704372	-0.05844315	-0.37262257
> 40K	-1.480071878	-2.095444235	-0.599449996	2.858762784
Cell's Contribution to Chi-Square	Very Dissatisfied	Somewhat Dissatisfied	Somewhat Satisfied	Very Satisfied
< 20K	1.499326463	0.026559799	0.099597859	0.914762153
20-30K	1.029733719	0.117919038	0.02139728	0.631873485
30-40K	0.581730668	1.035047535	0.00132216	0.057881515
> 40K	1.564416624	2.918900046	0.15970582	3.911611766

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#### Chi-Square Tests & Table Associations Ordinal Example: Satisfaction (Cols) & Salary (Rows)

Chi-Square	14.572			
DF	9			
P-Value	0.1034			
Additional Chi-Square Tests				
Test	Chi-Square	DF	P-Value	
Likelihood Ratio	15.4156	9	0.0801	
McNemar-Bowker Symmetry (Square Table)	32.8921	6	0.0000	
Measures of Association for Nominal Categories	antine a second			
Measure	Value	Std. Error	95% Lower Bound	95% Upper Boun
Pearson's Phi	0.2686			
Cramer's V	0.1551			
Contingency Coefficient	0.2594			
Cohen's Kappa (Agreement - Square Table)	0.0752	0.0428	-0.0087	0.159
Goodman-Kruskal Lambda (Cols Dependent)	0.0684	0.0547	0.0000	0.175
Goodman-Kruskal Lambda (Rows Dependent)	0.0296	0.0556	0.0000	0.138
Goodman-Kruskal Lambda (Symmetric)	0.0476	0.0483	0.0000	0.142
Goodman-Kruskal Tau (Cols Dependent)	0.0230	0.0136	0.0000	0.049
Goodman-Kruskal Tau (Rows Dependent)	0.0233	0.0115	0.0008	0.045
Theil's Uncertainty (Cols Dependent)	0.0322	0.0153	0.0022	0.062
Theil's Uncertainty (Rows Dependent)	0.0279	0.0134	0.0017	0.054
Theil's Uncertainty (Symmetric)	0.0299	0.0143	0.0019	0.057



#### Chi-Square Tests & Table Associations Ordinal Example: Satisfaction (Cols) & Salary (Rows)

Tests of Association for Ordinal Categories				
Test	Value	P-Value		
Concordant - Discordant	2707	0.0009		
Spearman Rank Correlation	0.2205	0.0016		
Measures of Association for Ordinal Categories				
Measure	Value	Std. Error	95% Lower Bound	95% Upper Bound
Spearman Rank Correlation	0.2205	0.0669	0.0834	0.3495
Kendall's Tau-B (Square Table)	0.1899	0.0570	0.0782	0.3017
Kendall-Stuart Tau-C (Rectangular Table)	0.1769	0.0535	0.0721	0.2817
Goodman-Kruskal Gamma	0.2700	0.0795	0.1141	0.4258
Somers' D (Cols Dependent)	0.1791	0.0540	0.0732	0.2850
Somers' D (Rows Dependent)	0.2014	0.0603	0.0833	0.3196
Somers' D (Symmetric)	0.1896	0.0569	0.0781	0.3012



## **Descriptive Statistics (Optional)**

- Percentile Report
  - 27 values from 0.135 to 99.865
- Percentile Ranges
  - 99.865 0.135 (99.73%, +/- 3 Sigma Equivalent)
  - 99.5 0.5 (99%)
  - 99 1 (98%)
  - 97.5 2.5 (95%, +/- 1.96 Sigma Equivalent)
  - 95 5 (90%, Span)
  - 90 10 (80%, Interdecile Range IDR)
  - 75 25 (50%, Interquartile Range IQR)



## **Descriptive Statistics (Optional)**

- Percentile Confidence and Tolerance Intervals
  - Interpolated or Exact
  - Minimum sample size reported if unable to compute CI or TI
  - Quartile Confidence Intervals (25, 50, 75)
  - Percentile Confidence Intervals (27 values from 0.135 to 99.865)
  - Percentile Tolerance Intervals (99.73%, 99%, 98%, 95%, 90%, 80%, 50%)
- Additional Descriptive Statistics
  - 5% Trimmed Mean
  - Standard Error of Mean
  - Variance
  - Coefficient of Variation
  - Short Term StDev (MR-bar/d2)



## **Descriptive Statistics (Optional)**

- Additional Normality Tests
  - Shapiro-Wilk (n <= 5000) and Kolmogorov-Smirnov-Lilliefors (n > 5000)
  - Doornik-Hansen
    - Univariate omnibus test based on Skewness and Kurtosis
    - Best for data with ties ("chunky" data)
- Outlier Tests
  - Boxplot: Potential 1.5(IQR), Likely 2.2(IQR), Extreme 3.0(IQR)
  - Grubbs
- Randomness Test
  - Nonparametric Runs Test (Exact)
- Normality, Outlier and Randomness Tests use the same Green, Yellow, Red highlight used in Version 7 hypothesis tests.



## Descriptive Statistics Example: Overall Satisfaction by Customer Type

Descriptive Statistics	Customer Type = 1	Customer Type = 2	Customer Type = 3
Count	31	42	27
Mean	3.394	4.205	3.641
Stdev	0.824680	0.621200	0.670478
Range	3.080	2.560	2.740
Minimum	1.720	2.420	2.190
25th Percentile (Q1)	2.810	3.828	3.240
50th Percentile (Median)	3.560	4.340	3.510
75th Percentile (Q3)	4.020	4.725	4.170
Maximum	4.800	4.980	4.930
95.0% CI Mean	3.0911 to 3.696	4.0117 to 4.3988	3.3759 to 3.9063
95.0% CI Sigma	0.65901 to 1.1023	0.51113 to 0.79213	0.52801 to 0.91884
Anderson-Darling Normality Test	0.312776	0.826259	0.389291
P-Value (A-D Test)	0.5306	0.0302	0.3600
Skewness	-0.235169	-0.967994	0.139571
P-Value (Skewness)	0.5557	0.0121	0.7411
Kurtosis	-0.671690	0.679609	-0.313701
P-Value (Kurtosis)	0.3705	0.2865	0.8435
Additiona	Descriptive Statistics		
5% Trimmed Mean	3.413	4.251	3.648
Standard Error of Mean	0.148117	0.095853182	0.129034
Variance	0.680097	0.385889	0.449541
Coefficient of Variation	24.301	14.772	18.414
StDev (Within, Short Term)	0.678487	0.521969	0.683988
Additio	nal Normality Tests		
Shapiro-Wilk/KSL	0.969383	0.923744	0.971664
P-Value (Shapiro-Wilk/KSL)	0.5022	0.0080	0.6463
Doornik-Hansen	0.813602	8.554	0.127399
P-Value (Doornik-Hansen)	0.6658	0.0139	0.9383



## Descriptive Statistics Example: Overall Satisfaction by Customer Type

Dverall Satisfaction by Customer Type Descriptive Statistics	Customer Type = 1	Customer Type = 2	Customer Type = 3
Descriptive outlates	Customer Type - 1	customer type - 2	customer type - 5
P	ercentile Report		
0.135	i 1.72	2.42	2.19
0.5	1.72	2.42	2.19
1	1.72	2.441	2.19
2.5	1.72	2.42	2.19
5	1.804	2.778	2.3
10	2.138	3.285	2.832
15	2.554	3.518	3.056
20		3.65	3.144
25	2.81	3.8275	3.24
30		3.981	3.272
35		4.091	3.298
40	3.074	4.132	3.3
45	3.248	4.3035	3.42
50	3.56	4.34	3.5
55	3.576	4.4195	3.566
60	3.804	4.464	3.644
65	i 3.9	4.5275	3.98
70	3.978	4.558	4.07
75	4.02	4.725	4.1
80	4.11	4.786	4.29
85	4.242	4.881	4.42
90		4.91	4.68
95	i 4.722	4.9655	4.87
97.5	4.8	4.97925	4.9
99	4.8	4.98	4.9
99.5	4.8	4.98	4.9
99.865	4.8	4.98	4.9
75 - 25 (50%, Interquartile Range IQR)	3.08	2.56	2.7
90 - 10 (80%, Interdecile Range IDR	3.08	2.56	2.7
95 - 5 (90%, Span	3.08	2.539	2.7
97.5 - 2.5 (95%, +/- 1.96 Sigma Equivalent	3.08	2.55925	2.7
99 - 1 (98%)		2.1875	2.50
99.5 - 0.5 (99%	2.448	1.625	1.85
99.865 - 0.135 (99.73%, +/- 3 Sigma Equivalent		0.8975	0.93



## **Descriptive Statistics Example: Overall Satisfaction by Customer Type**

Customer Type = 3

**Overall Satisfaction by Customer Type Descriptive Statistics** Customer Type = 1 Customer Type = 2

	nce Intervals (Interpolate		
	Min. sample size = 2731	Min. sample size = 2731	Min. sample size = 2731
0.5	Min. sample size = 736		Min. sample size = 736
1	Min. sample size = 368		Min. sample size = 368
2.5	Min. sample size = 146		Min. sample size = 146
5	Min. sample size = 72	Min. sample size = 72	Min. sample size = 72
10	Min. sample size = 36	2.5826 to 3.6589	Min. sample size = 36
15	1.8393 to 2.9095	3.1206 to 3.8676	2.4389 to 3.2707
20	2.0087 to 2.9711	3.2747 to 4.0232	2.7108 to 3.3014
25	2.4809 to 3.1075	3.4847 to 4.1163	2.9143 to 3.3899
30	2.5606 to 3.2586	3.5891 to 4.3005	3.0606 to 3.4556
35	2.6047 to 3.5658	3.7308 to 4.3359	3.1354 to 3.5275
40	2.7749 to 3.6297	3.8487 to 4.4153	3.2052 to 3.6277
45	2.906 to 3.817	3.9942 to 4.4601	3.2554 to 3.862
50	2.9535 to 3.9362	4.0946 to 4.5184	3.2891 to 4.0227
55	3.0221 to 3.987	4.1397 to 4.5458	3.3036 to 4.1239
60	3.2061 to 4.0266	4.3049 to 4.6959	3.3845 to 4.1874
65	3.387 to 4.1066	4.3441 to 4.7459	3.4401 to 4.3391
70	3.5707 to 4.2345	4.4284 to 4.8516	3.5236 to 4.4274
75	3.7743 to 4.2921	4.4737 to 4.8928	3.626 to 4.6107
80	3.8978 to 4.67	4.53 to 4.91	3.9334 to 4.7587
85	3.9853 to 4.6892	4.6717 to 4.9457	4.0779 to 4.8581
90	Min. sample size = 36	4.77 to 4.9742	Min. sample size = 36
95	Min. sample size = 72	Min. sample size = 72	Min. sample size = 72
97.5	Min. sample size = 146	Min. sample size = 146	Min. sample size = 146
99	Min. sample size = 368	Min. sample size = 368	Min. sample size = 368
99.5	Min. sample size = 736	Min. sample size = 736	Min. sample size = 736
99.865	Min. sample size = 2731	Min. sample size = 2731	Min. sample size = 2731
		1	0
Percentile Tolerance In	tervals (Interpolated 95.0	)% Minimum)	
50%	2.56 to 4.1129	3.62 to 4.8262	3.04 to 4.2764
80%	1.7453 to 4.67	3.108 to 4.97	2.4552 to 4.93
90%	Min. sample size = 46	Min. sample size = 46	Min. sample size = 46
95%	Min. sample size = 93	Min. sample size = 93	Min. sample size = 93
98%	Min. sample size = 236	Min. sample size = 236	Min. sample size = 236
99%	Min. sample size = 473	Min. sample size = 473	Min. sample size = 473
99.73%	Min. sample size = 1756	Min. sample size = 1756	



## Descriptive Statistics Example: Overall Satisfaction by Customer Type

**Overall Satisfaction by Customer Type Descriptive Statistics** Customer Type = 1 Customer Type = 2Customer Type = 3**Outlier and Randomness Tests** Potential (1.5\*IQR) **Outliers (Boxplot Rules)** No outliers found outlier lower count = 1 No outliers found Grubbs' Test P-Value = Grubbs' Test P-Value = Grubbs' Test P-Value = 0.105. Fail to reject 1.000. Fail to reject 0.654. Fail to reject null hypothesis: "There null hypothesis: "There null hypothesis: "There are no outliers in the are no outliers in the are no outliers in the data set." Note that data set." Note that data set." Note that Grubbs' Test assumes Grubbs' Test assumes Grubbs' Test assumes normality and tests normality and tests normality and tests only if the maximum or only if the maximum or only if the maximum or minimum is an outlier. minimum is an outlier. minimum is an outlier Grubbs Outlier Test Nonparametric Runs Nonparametric Runs Nonparametric Runs Test (Exact) P-Value = Test (Exact) P-Value = Test (Exact) P-Value = 0.066. Fail to reject 1.000. Fail to reject 1.000. Fail to reject null hypothesis: "data null hypothesis: "data null hypothesis: "data are random." so are random." so are random," so conclude that the conclude that the conclude that the assumption of assumption of assumption of randomness randomness randomness (independence) is not (independence) is not (independence) is not Randomness Runs Test violated violated. violated



- 1 Sample Z test and Confidence Interval for Mean
- Tolerance Interval Calculator (Normal Exact)
- Equivalence Tests Two One-Sided Tests (TOST)
  - 1 Sample Equivalence Test for Mean
  - 2 Sample Equivalence Test (Compare 2 Means)
  - 2 Proportions Equivalence Test
  - 2 Poisson Rates Equivalence Test
- Type 1 Gage Study
- Gage Bias and Linearity Study



## **Tolerance Interval Calculator** (Normal Exact)

Sigma XL	Tolerance Interval Calculator (Normal Exact)		
	Sample Data (user inputs)		11:
	Sample Size	n	30
	Sample Mean	x-bar	1
	Sample Standard Deviation	5	1
	Population Coverage (enter .99 for 99%)	100*(p)%	99.0%
	Confidence Level (enter .95 for 95%)	<b>100*(1-α)%</b>	95.0%
	Tolerance Interval Type		Two-Sided

Results:	
Upper Tolerance Limit	4.3546
Lower Tolerance Limit	-2.3546



## 2 Sample Equivalence Test (Compare 2 Means)

Sample Data (user inputs):		Test/Treatment Sample	Reference/Contro Sample	
Sample Size	n	30	30	
Sample Mean	x-bar	0.0000	0.5000	
Sample Standard Deviation	S	1.0000	1.0000	
Upper Equivalence Limit	UEL		1.0	
Lower Equivalence Limit	LEL		1.0	
Confidence Level (enter .95 for 95%)	100*(1-α)%	95	95.0%	
Assume Equal Variances		Yes		
	Results:			
Sample M	ean Difference	-0.	5000	
Standard Error Difference (using po	ooled variance)	0.:	2582	
df (	equal variance)	58		
¢.	alpha	0.0500		
t1-s	statistic (upper)	-5.8095		
t2-	statistic (lower)	1.9365		
P1-Value (upper)		0.0000		
P2-Value (lower)		0.0288		
Equivalence P-Value (maximu	m of P1 and P2)	0.	0288	
Upper Confidence Limit M	ean Difference	-0.	0684	
Lower Confidence Limit Mean Difference		-0.9316		

Interpretation of p-value and Confidence Intervals

Since the Equivalence P-Value is less than alpha (0.05), conclude that equivalence is true.

Since the 95% confidence interval is within the equivalence interval, conclude that equivalence is true.

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#### Type 1 Gage Study

Gage Name:	Example Type 1 Gage Study
Date of Study:	
Performed By:	
Notes:	

Tolerance (Tol, USL - LSL):	0.2
Part Reference Value (Ref):	10
Gage Resolution:	0.0001
StDev Multiplier:	6.00
Percent of Tolerance for Cg/Cgk:	20

Trial:	<u>Measurement Data</u>			
1	10.0063			
2	10.0014			
3	9.9945			

Count	50
Mean	10.00071
StDev	0.004149
StDev*Multiplier (SV)	0.024893
Ref + 0.1*Tol	10.02
Ref - 0.1*Tol	9.98

Type 1	Gage	Run	Chart
Type I	Juge	Null	Chart

Bias	0.00071
Bias t-Statistic	1.210106
Bias P-Value	0.2320
Gage Capability Cg	1.61
Gage Capability Cgk	1.55
Gage Repeatability % (100*SV/Tol)	12.45%
Gage Repeatability & Bias % (20/Cgk)	12.90%
Resolution % of Tolerance	0.05%



## **Gage Bias & Linearity Study**

	ampic ouger	bias and Linea	arity Study - AIAG	MSA Referenc	e Manual, 4th Editi	on, Page 99					
Date of Study: Performed By: Notes:											
Process Variation (SV from Gage R&R or 6 * Historical StDev):	10		Gage Linearity	Report							
Part:	1	2	3	4	5	Part:	1	2	3	4	
Reference Value:	2	4	6	8	10	Reference Value:	2	4	6	8	
Trial			<u> </u>		<u> </u>	Trial		Bias C	Calculations		
11	2.7	5.1	5.8	7.6	9.1	11	0.7	1.1	-0.2	-0.4	1
2	2.5	3.9	5.7	7.7	9.3	2	0.5	-0.1	-0.3	-0.3	
3	2.4	4.2	5.9	7.8	9.5	3	0.4	0.2	-0.1	-0.2	
4	2.5	5	5.9	7.7	9.3	4	0.5	1	-0.1	-0.3	
5	2.7	3.8	6	7.8	9.4	5	0.7	-0.2	0	-0.2	
6	2.3	3.9	6.1	7.8	9.5	6	0.3	-0.1	0.1	-0.2	
7	2.5 2.5	3.9	6	7.8	9.5	7	0.5	-0.1	0	-0.2 -0.3	
8	2.5	3.9 3.9	6.1 6.4	7.7	9.5 9.6	8	0.5	-0.1 -0.1	0.1	-0.3	
10	2.4		6.3	7.5	9.0	10	0.4	-0.1	0.4	-0.2	
10	2.4	4.1	6	7.6	9.3	10	0.4	0.1	0.5	-0.4	
12	2.4	3.8	6.1	7.7	9.4	12	0.4	-0.2	0.1	-0.3	
13	2.1	5.5	0.1		0.4	13	0.1	0.2	0.1	0.0	-
14						14					-
15						15				-	
16						16					<u> </u>
17						17					
18						18					
19						19					
						20					



## **Gage Bias & Linearity Study**

Bias	0.491666667	0.125	0.025	-0.291666667	-0.616666667
% Bias	4.92%	1.25%	0.25%	2.92%	6.17%
P-Value	0.0000	0.3540	0.6671	0.0000	0.0000

R-Square	71.43%
Adj, R-Square	70.94%
StDev	0.239539789
Linearity	1.316666667
% Linearity	13.17%

**P-Value** 

**Average Bias** 

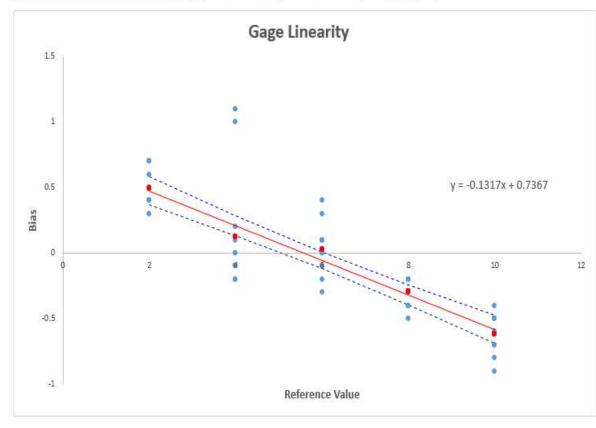
% Average Bias

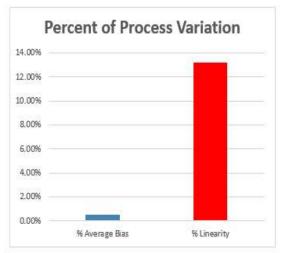
-0.053333333

0.53%

0.0894

	Coeff	SE Coeff	P-Value
Constant	0.736666667	0.072524273	0.0000
Siope	-0.131666667	0.010933445	0.0000







## Why SigmaXL?

- Measure, Analyze, and Control your Manufacturing, Service, or Transactional Process.
- An add-in to the already familiar Microsoft Excel, making it a great tool for Lean Six Sigma training. Used by Motorola University and other leading consultants.
- SigmaXL is rapidly becoming the tool of choice for Quality and Business Professionals.



# What's Unique to SigmaXL?

- User-friendly Design of Experiments with "view power analysis as you design".
- Measurement Systems Analysis with Confidence Intervals.
- Two-sample comparison test automatically tests for normality, equal variance, means, and medians, and provides a rules-based yellow highlight to aid the user in interpretation of the output.
- Low p-values are highlighted in red indicating that results are significant.



# What's Unique to SigmaXL?

- Template: Minimum Sample Size for Robust Hypothesis Testing
  - It is well known that the central limit theorem enables the t-Test and ANOVA to be fairly robust to the assumption of normality.
  - A question that invariably arises is, "How large does the sample size have to be?"
  - A popular rule of thumb answer for the one sample t-Test is "n = 30." While this rule of thumb often does work well, the sample size may be too large or too small depending on the degree of non-normality as measured by the Skewness and Kurtosis.
  - Furthermore it is not applicable to a One Sided t-Test, 2 Sample t-Test or One Way ANOVA.
  - To address this issue, we have developed a unique template that gives a minimum sample size needed for a hypothesis test to be robust.



# What's Unique to SigmaXL?

- Powerful Excel Worksheet Manager
  - List all open Excel workbooks
  - Display all worksheets and chart sheets in selected workbook
  - Quickly select worksheet or chart sheet of interest
- Process Capability and Control Charts for Nonnormal data
  - Best fit automatically selects the best distribution or transformation!
  - Nonnormal Process Capability Indices include Pp, Ppk, Cp, and Cpk
  - Box-Cox Transformation with Threshold so that data with zero or negative values can be transformed!



## **Recall Last Dialog**

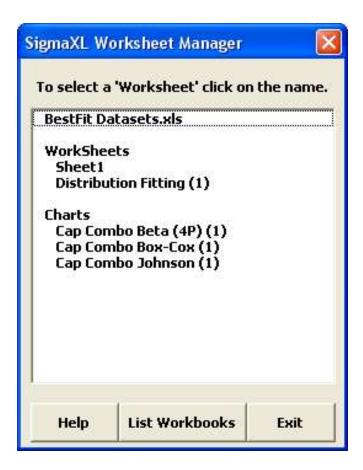
#### Recall SigmaXL Dialog

- This will activate the last data worksheet and recall the last dialog, making it very easy to do repetitive analysis.
- Activate Last Worksheet
  - This will activate the last data worksheet used without recalling the dialog.



## **Worksheet Manager**

- List all open Excel workbooks
- Display all worksheets and chart sheets in selected workbook
- Quickly select worksheet or chart sheet of interest





## **Data Manipulation**

- Subset by Category, Number, or Date
- Random Subset
- Stack and Unstack Columns
- Stack Subgroups Across Rows
- Standardize Data
- Random Number Generators
  - Normal, Uniform (Continuous & Integer), Lognormal, Exponential, Weibull and Triangular.
- Box-Cox Transformation



- DMAIC & DFSS Templates:
  - Team/Project Charter
  - SIPOC Diagram
  - Flowchart Toolbar
  - Data Measurement Plan
  - Cause & Effect (Fishbone) Diagram and Quick Template
  - Cause & Effect (XY) Matrix
  - Failure Mode & Effects Analysis (FMEA)
  - Quality Function Deployment (QFD)
  - Pugh Concept Selection Matrix
  - Control Plan



### • Lean Templates:

- Takt Time Calculator
- Value Analysis/Process Load Balance
- Value Stream Mapping
- Basic Graphical Templates:
  - Pareto Chart
  - Histogram
  - Run Chart



- Basic Statistical Templates:
  - Sample Size Discrete and Continuous
  - Minimum Sample Size for Robust t-Tests and ANOVA
  - 1 Sample t-Test and Confidence Interval for Mean
  - 2 Sample t-Test and Confidence Interval (Compare 2 Means) with option for equal and unequal variance
  - 1 Sample Chi-Square Test and CI for Standard Deviation
  - 2 Sample F-Test and CI (Compare 2 Standard Deviations)
  - 1 Proportion Test and Confidence Interval
  - 2 Proportions Test and Confidence Interval



- Basic Statistical Templates:
  - 1 Poisson Rate Test and Confidence Interval
  - 2 Poisson Rates Test and Confidence Interval
  - One-Way Chi-Square Goodness-of-Fit Test
  - One-Way Chi-Square Goodness-of-Fit Test Exact
- Probability Distribution Calculators:
  - Normal, Lognormal, Exponential, Weibull
  - Binomial, Poisson, Hypergeometric



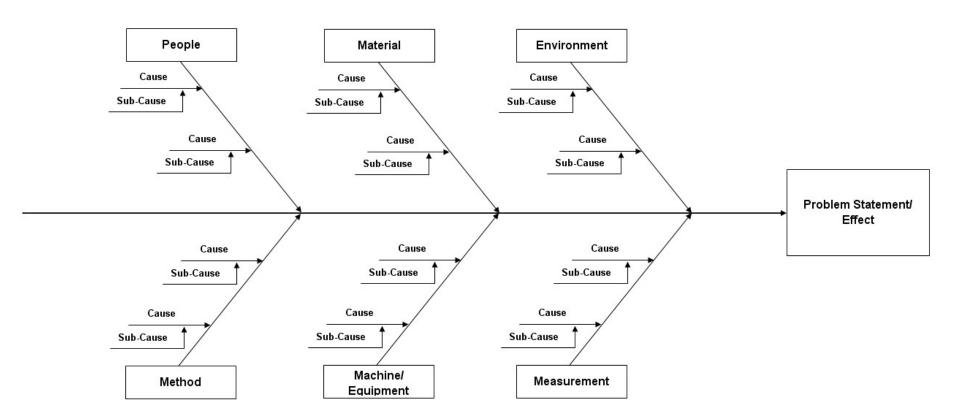
- Basic MSA Templates:
  - Gage R&R Study with Multi-Vari Analysis
  - Attribute Gage R&R (Attribute Agreement Analysis)
- Basic Process Capability Templates:
  - Process Sigma Level Discrete and Continuous
  - Process Capability & Confidence Intervals
- Basic DOE Templates:
  - 2 to 5 Factors
  - 2-Level Full and Fractional-Factorial designs
  - Main Effects & Interaction Plots
- Basic Control Chart Templates:
  - Individuals
  - C-Chart



## Templates & Calculators: Cause & Effect Diagram

**CAUSE & EFFECT (FISHBONE) DIAGRAM** 

Process/Project Name:	
Date:	ĩ
Prepared By:	
Notes:	





## Templates & Calculators: Quality Function Deployment (QFD)

			/	+++		X	X	X	X	$\left<\right>$	$\left>\right>$							
	Desired Direction of Improve	mont	$\bigcap^{+}$	+ <u> </u>	- ×+ ↑	<b>+</b> × ↑	$\square$	$\bigwedge$	$\bigwedge$	$\bigwedge$	$\bigwedge$	$\stackrel{>}{\sqcap}$	]					
	Desired Direction of Improve	ment.			Fur	nctiona	l Req	lireme	ents (Ho	w):	I			Satis	factio	n Ratii	nqs:	
	Customer Requirements (What):	Customer Importance Rating	Functional Requirement 1	Functional Requirement 2	Functional Requirement 3	Functional Requirement 4	Functional Requirement 5	Functional Requirement 6	Functional Requirement 7	Functional Requirement 8	Functional Requirement 9	Functional Requirement 10	Our Customer Satisfaction (CS) Rating	Competitor 1 Rating	Competitor 2 Rating	Competitor 3 Rating	Competitor 4 Rating	CS - Mas(Competitor Rating)
_	Customer Requirements (what):	4	9	3	LL.	9	ш	ш	ш.	ш	ш	ш.	3	2	0	0	0	1
-	Customer Requirement 2	5	9	9	9	9							4	4				0
+ +++	Customer Requirement 3	2	3	3	1	9							4	3				1
+	Customer Requirement 4	3	9	1	1	9							1	3				-2
	Customer Requirement 5																	0
	Customer Requirement 6																	0
	Customer Requirement 7																	0
	Customer Requirement 8																	0
	Customer Requirement 9																	0
$\times$	Customer Requirement 10																	0
	Raws	Score:	114	66	50	126	0	0	0	0	0	0						
		Rank:	2	3	4	1	5	5	5	5	5	5						



## Templates & Calculators: Pugh Concept Selection Matrix

Key Criteria	Weight	Concept A	Concept B	Concept C	Concept D	Concept E	Concept F	Concept G	Concept H	Concept I	Concept J	Current Baseline Datum
Criterion 1	4	+	S	-								S
Criterion 2	5	+	S	S	9							S
Criterion 3	3	S	+									S
Criterion 4	2	+	S	S								S
Criterion 5	5	+	+	S								S
Criterion 6										1.2		s
Criterion 7												s
Criterion 8	2	20 50										S
Criterion 9												s
Criterion 10	63											s
Criterion 11	23 10											S
Criterion 12												S
Criterion 13	10											S
Criterion 14												S
Criterion 15												s
Criterion 16	6. 2											s
Criterion 17												s
Criterion 18	62											s
Criterion 19	20 10											S
Criterion 20												S
	200 12					a a u u					int da Da da	
Sum of Pos			2	0	0	0	0	0	0	0	0	
Sum of Ne	gatives(-): Sames (S):	0	0	2	0	0	0	0	0	0	0	
Positives - N		4	2	-2	0	0	0	0	0	0	0	
1 0311763 - 1	reguires.	-	-	-2		0	0	v	v	v	0	1
Weighted Sum of Pos			8	0	0	0	0	0	0	0	0	]
Weighted Sum of Neg	gatives (-):	0	0	7	0	0	0	0	0	0	0	
Weighted Sum of S	ames (S):	3	11	12	0	0	0	0	0	0	0	
Weighted Positives - Weighted N	legatives:	16	8	-7	0	0	0	0	0	0	0	

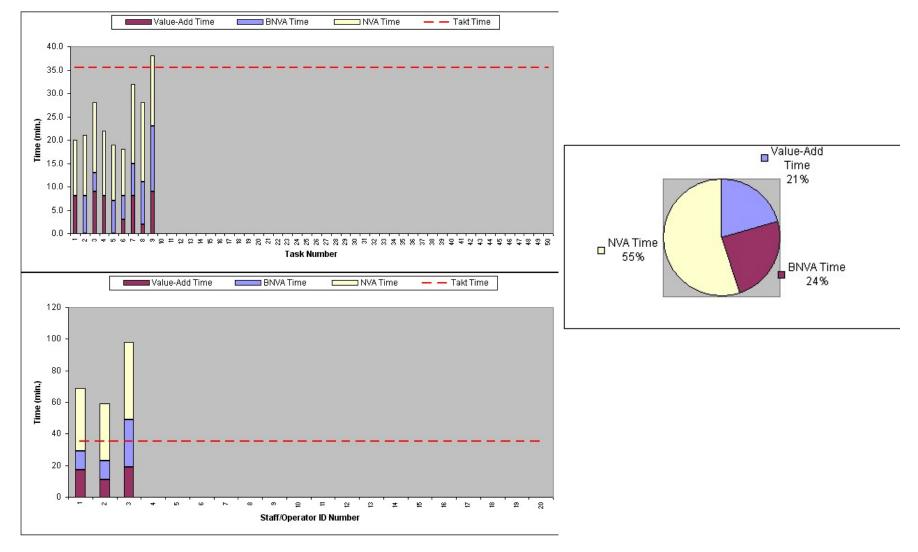


## Templates & Calculators: Lean Takt Time Calculator

SigmaXL Lean Templates: Tal	t Time Calculator	
Daily Customer Demand:	units per day	22
Scheduled Work:	hours per shift	8
Shifts per Day:		2
Lunch:	minutes per shift	30
Breaks:	minutes per shift	30
Planned Downtime:	minutes per shift	30
Staff/Operator Cycle Time:	minutes per unit	226
		<u></u>
Available Time:	minutes per day	780.0
Takt Time:	minutes per unit	35.5
Required Number of Staff/Op	erators:	6.4



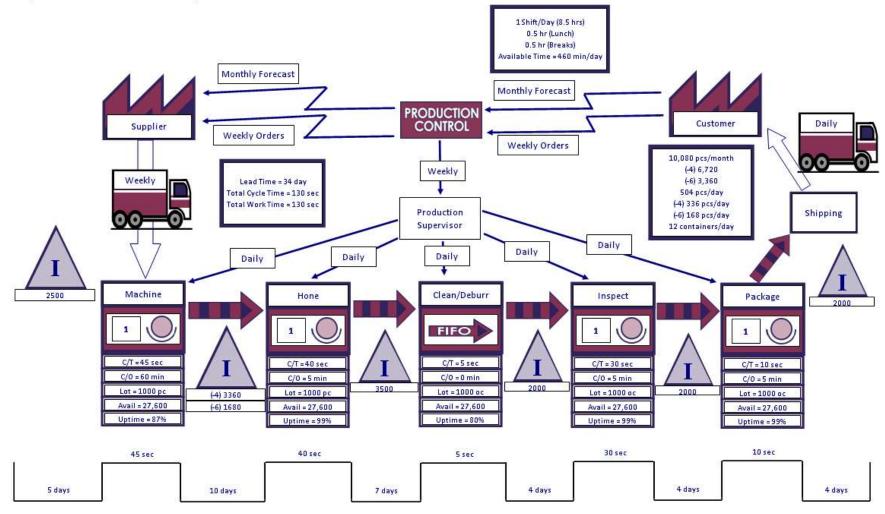
## Templates & Calculators: Value Analysis/ Process Load Balance Chart





## Templates & Calculators: Value Stream Mapping

Example Present State Value Stream Map





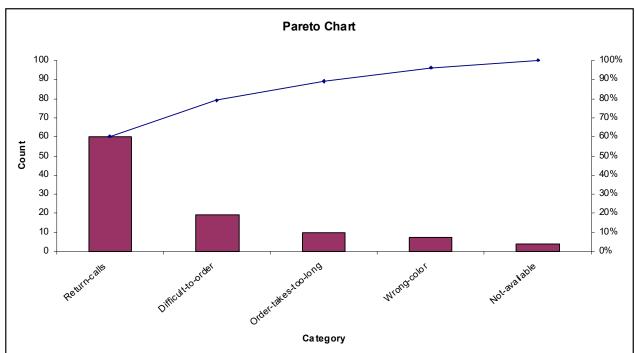
## Templates & Calculators: Pareto Chart Quick Template

A	В	С	
Category	<u>Count</u>		
Difficult-to-order	19		
Not-available	4		
Order-takes-too-long	10		
Return-calls	60		
Wrong-color	7		
		A	Par
		3.	

Pareto Chart

D

Е





## Templates & Calculators: Failure Mode & Effects Analysis (FMEA)

#### Potential Failure Mode & Effects Analysis

	R	ess/Product: <u>Ir</u> FMEA Team: esponsibility: Prepared By:	nventory Mar	nagement					
	8			5.	Process				
Process Steps or Product Functions	Potential Failure Mode	Potential Effec	ts of Failure	Severity (1-10)	Potential Cause(s) of Failure	Occurrence (1-10)	Current Controls	Detection (1-10)	Risk Priority Number (RPN)
Stock inventory	Stock in wrong location	Unable to loca	ate stock	5	Correct location is full	7	Stock checked twice a year	9	315

Score		Severity Guidelines						
		AIAG	Six Sigma					
	10 Hazar	dous without warning	Injure a customer or employee	E				
	9 Hazar	dous with warning	Be illegal					
	8 Very H	ligh	Render product or service unfit for use					
	7 High	10.00	Cause extreme customer dissatisfaction					
	6 Moder	rate	Result in partial malfunction					
	5 Low		Cause a loss of performance which is likely to result in a complaint					
	4 Very L	_OW	Cause minor performance loss					
	3 Minor		Cause a minor nuisance but can be overcome with no performance loss					
	2 Very M	Minor	Be unnoticed and have only minor effect on performance					
	1 None		Be unnoticed and not affect the performance	G				



#### Templates & Calculators: Cause & Effect (XY) Matrix

Δ

#### CAUSE & EFFECT (XY) MATRIX

V/A

Process/Project Name:	Call Center Example
Date:	
Performed By:	
Notes:	

Output Variables (Y's): Importance Score (1-10):	Call Abandon Rate 8	Customer Satisfaction 10	Y3	¥4	Y5	Y6	Y7	Y8	Y9	Y10	
Input/Process Variables (X's)				Table of	Association	Scores (X's	to Y's)				Weighted Score
Answer Speed	9	9									162
Employee Experience	1	3									38
First Time Resolution	0	9									90



## Templates & Calculators: Sample Size Calculators

Sigma Sample Size Calculat	tor - Discrete Data	
Sample Data (u	ser inputs):	
Estimate of Proportion	P	0.5
Desired margin of error	delta / half-interval	0.03
Population Size (optional)	N	
Confidence level (enter .95 for 95%)	100*(1-α)%	95.0%
Result	ts:	
Minimum Sample Size	n	1068
	n (adjusted for small N)	
	np check (should be ≥ 5)	534



## Templates & Calculators: Sample Size Calculators

Sigma Sample Size Calculator	r - Continuous Data	
Sample Data (us	ser inputs):	-
Estimate of Standard Deviation	S	1
Desired margin of error	delta / half-interval	0.25
Population Size (optional)	N	
Confidence level (enter .95 for 95%)	100*(1-α)%	95.0%
Result	s:	
Minimum Sample Size	n	62
	n (adjusted for small N)	



## Templates & Calculators: Minimum Sample Size for Robust Hypothesis Testing

Minimum Sample Size for R	obust Hypothesis	Testing
Sample Data (	user inputs):	*
Hypothesis Test:		1 Sample t-Test
Alternative Hypothesis :	Ha	Not Equal To
Confidence Level:	100*(1-α)%	95%
Skewness:	Skew	1
Kurtosis:	Kurt	-0.48
Resu	lts:	~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~
Minimum sample size for each sample/group:	n	30



#### Templates & Calculators: Process Sigma Level – Discrete

Sigma Process Sigma Level Calculator	r - Discre	te Data
Sample Data (user input	uts):	
Number of units	n	500
Total number of defects observed	d	5
Number of defect opportunities per unit	0	1
Sigma Shift (typically +1.5 for long term data)		1.5
Results:		~
Defects per Unit	dpu	0.01
Defects per Million Opportunities	dpmo	10,000.0
Defects per Opportunity	dpo%	1.00%
Yield	yield%	99.00%
Process Sigma Level	sigma	3.826



#### Templates & Calculators: Process Sigma Level – Continuous

Sigma Process Sigma Level Calculator - Continuou	
(Assumes that data are normally distributed)	
Sample Data (user inputs):	
Mean x-bar	0
Standard Deviation s	1
Upper Specification Limit USL	3
Lower Specification Limit LSL	-3
Sigma Shift (typically +1.5 for long term data)	1.5
	*
Results:	
Expected dpm > USL	1349.9
Expected % > USL	0.13%
Expected dpm < LSL	1349.9
Expected % < LSL	0.13%
Expected dpm (overall)	2699.8
Expected yield (overall) %	99.73%
Process Sigma Level	4.282



#### Templates & Calculators: 2 Proportions Test and Confidence Interval

Sigma 2 Proportions Test an	d Confidence	Interval	
Sample Data (user inputs):		Sample 1	Sample 2
Number of Events	x	1	2
Sample Size	n	10	10
Null Hypothesis (hypothesized difference)	$H_0: P_1 - P_2 =$		0
Alternative Hypothesis	H <sub>a</sub> : P <sub>1</sub> - P <sub>2</sub>	Not Ed	qual To
Confidence Level (enter .95 for 95%)	100*(1-α)%	95.	.0%
Hypothesis Test Method		Fisher	s Exact
Confidence Interval Method		Newcombe-Wilson Score	
Res	ults:		
Sample	proportion (x/n)	0.1000	0.2000
Sample prop	ortion difference	-0.1	000
	alpha	0.0	500
Minimum expected value (should be >= 5 for norma	al approximation)	1.5	000
Fisher's Exact probability	p-value (2-sided)	1.0	000
Upper Confidence	ce Limit (2-sided)	0.2	362
Lower Confidence	ce Limit (2-sided)	-0.4	205

	Test Informa	tion
Null Hypothesis H <sub>0</sub> :	$P_1 - P_2 = 0$	Fail to Reject
Alternative Hypothesis H <sub>a</sub> :	$P_1 - P_2 \neq 0$	



#### Templates & Calculators: Normal Distribution Probability Calculator

Sigma Normal Distribution Probability	Calcula	tor
Input the following information:		
Mean	μ	0
Standard Deviation	σ	1
Lower Bound (or LSL)	X1	1
Upper Bound (or USL)	X2	2

Areas:	Select the Prob the following pr	ability of Interest from obabilities:	
between X1 and X2		Prob( 1 ≤ X ≤ 2 )	0.135905122
outside X1 and X2	X1 X2	Prob(X≤1 AND X≥2)	0.864094878
below X1		Prob(X≤1)	0.841344746
above X1	XI	Prob(X≥1)	0.158655254
below X2		Prob( X ≤ 2 )	0.977249868
above X2		Prob(X≥2)	0.022750132



## **Graphical Tools**

- Basic and Advanced (Multiple) Pareto Charts
- EZ-Pivot/Pivot Charts
- Run Charts (with Nonparametric Runs Test allowing you to test for Clustering, Mixtures, Lack of Randomness, Trends and Oscillation.)
- Basic Histogram
- Multiple Histograms and Descriptive Statistics (includes Confidence Interval for Mean and StDev., as well as Anderson-Darling Normality Test)
- Multiple Histograms and Process Capability (Pp, Ppk, Cpm, ppm, %)

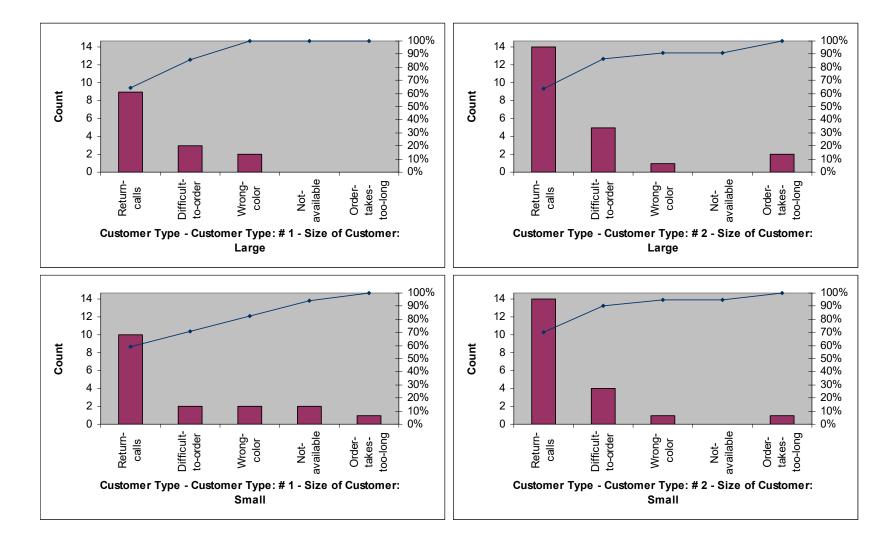


## **Graphical Tools**

- Multiple Boxplots and Dotplots
- Multiple Normal Probability Plots (with 95% confidence intervals to ease interpretation of normality/non-normality)
- Multi-Vari Charts
- Scatter Plots (with linear regression and optional 95% confidence intervals and prediction intervals)
- Scatter Plot Matrix



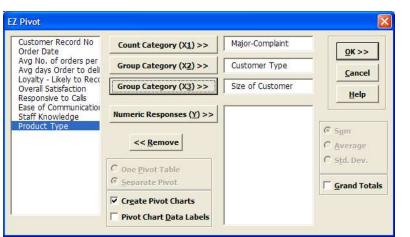
## **Graphical Tools: Multiple Pareto Charts**



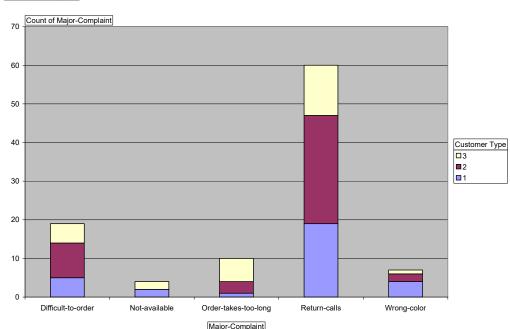


Graphical Tools: EZ-Pivot/Pivot Charts – The power of Excel's Pivot Table and Charts are now easy to use!

Size of Customer (All)

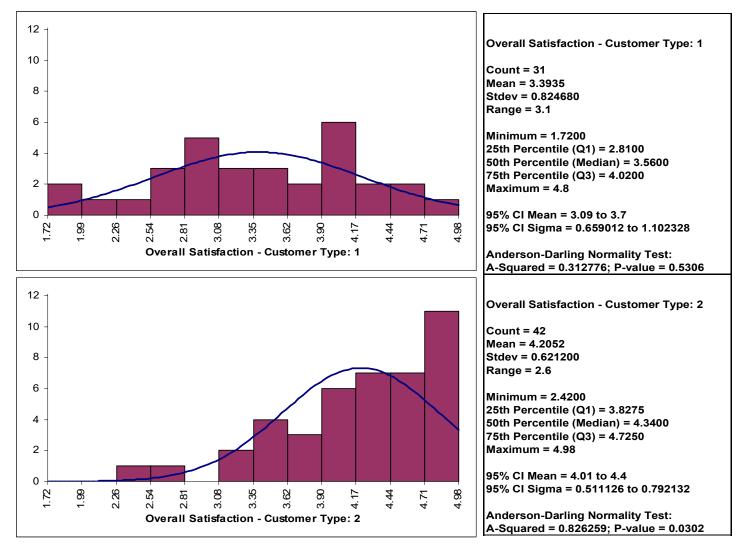


Size of Customer	(All)	-	-
Count of Major-Complaint	Customer Type	-	
Major-Complaint -		1 2	3
Difficult-to-order	11	59	5
Not-available		2	2
Order-takes-too-long		1 3	6
Return-calls	1	9 28	13
Wrong-color	1. A	4 2	1



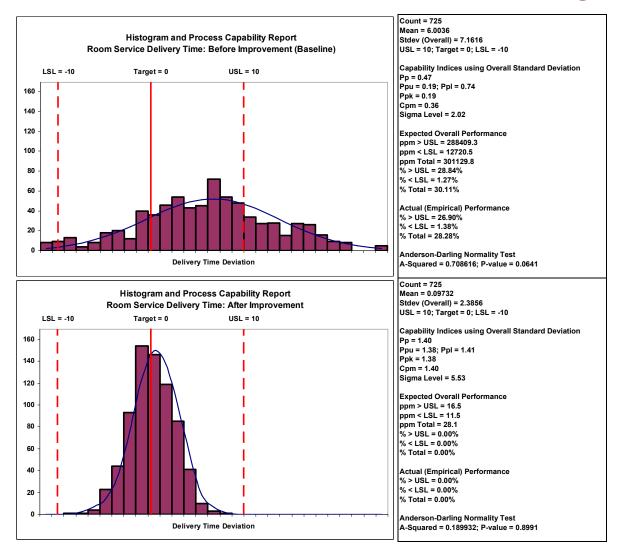


### Graphical Tools: Multiple Histograms & Descriptive Statistics



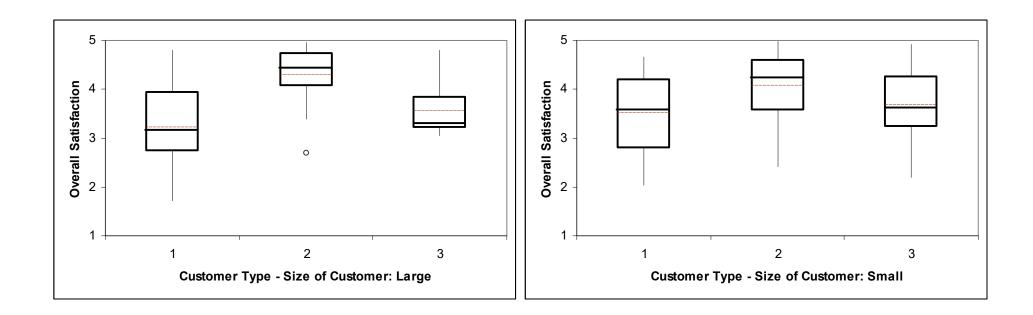


### Graphical Tools: Multiple Histograms & Process Capability



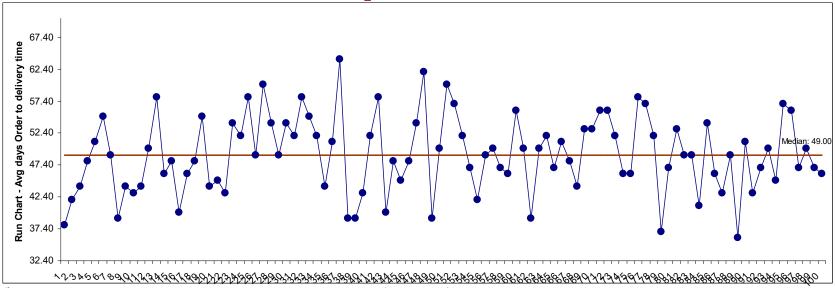


## **Graphical Tools: Multiple Boxplots**





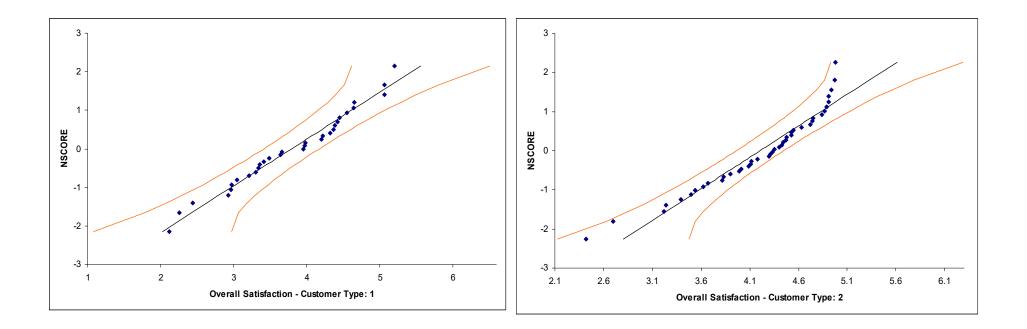
### **Graphical Tools: Run Charts with Nonparametric Runs Test**



Nonparametric Runs Test: Avg days Order to delivery time	
Number of Runs about Median:	45
Expected Number of Runs about Median:	50.68
Number of Points above Median:	46
Number of Points equal to or below Median:	54
P-Value for Clustering:	0.1252
P-Value for Mixtures:	0.8748
P-Value for Lack of Randomness (2-Sided):	0.2505
Number of Runs Up or Down:	60
Expected Number of Runs Up or Down:	66.33333
P-Value for Trends:	0.0648
P-Value for Oscillation:	0.9352

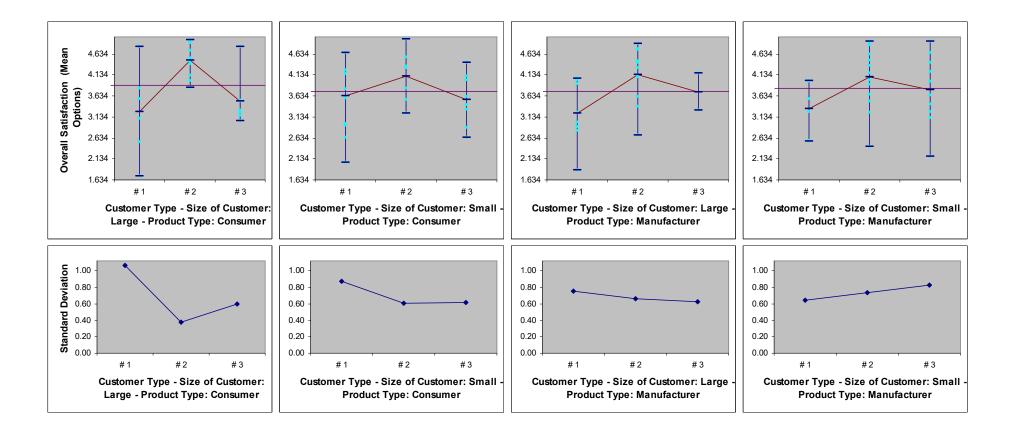


### **Graphical Tools: Multiple Normal Probability Plots**



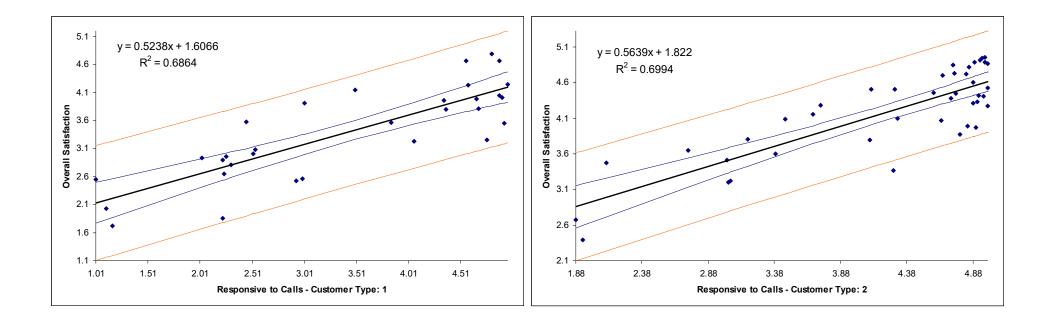


## **Graphical Tools: Multi-Vari Charts**





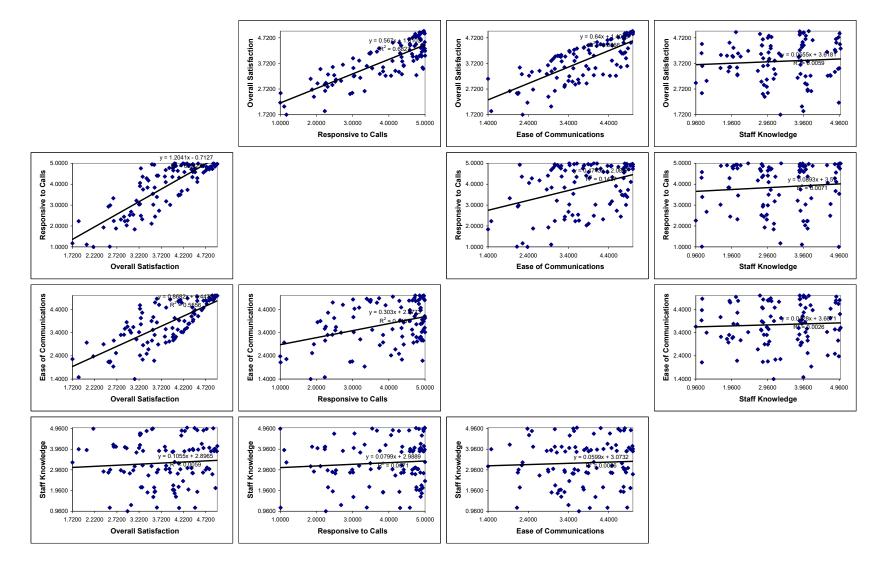
### Graphical Tools: Multiple Scatterplots with Linear Regression



Linear Regression with 95% Confidence Interval and Prediction Interval



## **Graphical Tools: Scatterplot Matrix**





- P-values turn red when results are significant (pvalue < alpha)</li>
- Descriptive Statistics including Anderson-Darling Normality test, Skewness and Kurtosis with pvalues
- 1 Sample t-test and confidence intervals
  - Optional Assumptions Report
- Paired t-test, 2 Sample t-test
  - Optional Assumptions Report



- 2 Sample Comparison Tests
  - Normality, Mean, Variance, Median
  - Yellow Highlight to aid Interpretation
- One-Way ANOVA and Means Matrix
  - Optional Assumptions Report
- Two-Way ANOVA
  - Balanced and Unbalanced



- Equal Variance Tests:
  - Bartlett
  - Levene
  - Welch's ANOVA (with optional assumptions report)
- Correlation Matrix
  - Pearson's Correlation Coefficient
  - Spearman's Rank
  - Yellow highlight to recommend Pearson or Spearman based on bivariate normality test



- Multiple Linear Regression
- Binary and Ordinal Logistic Regression
- Chi-Square Test (Stacked Column data and Two-Way Table data)
- Chi-Square Fisher's Exact and Monte Carlo Exact



- Nonparametric Tests
- Nonparametric Tests Exact and Monte Carlo Exact
- Power and Sample Size Calculators
- Power and Sample Size Charts



### Statistical Tools: Two-Sample Comparison Tests

Customer Type	1	2
Count	31	42
Mean	3.3935	4 2052
Median	3,5600	4.3400
Standard Deviation	0 824680	0.621200
AD Normality Test p-value	0.5306	0.0302
Test for Equal Variances:		
F-test (use with normal data):		
F	1.7624	
p-value (2-sided)	0.0916	
Levene's test (use with non-normal data):		
p-value (2-sided)	0.0443	
2 Sample t-test for means:		
	2° 7	
Assume Equal Variance:		
t	-4.7991	
t p-value (2-sided)	0.0000	
t		
t p-value (2-sided)	0.0000	
t p-value (2-sided) p-value (1-sided)	0.0000	
t p-value (2-sided) p-value (1-sided) Assume Unequal Variance:	0.0000	
t p-value (2-sided) p-value (1-sided) Assume Unequal Variance: t	0.0000 0.0000 -4.6007	
t p-value (2-sided) p-value (1-sided) Assume Unequal Variance: t p-value (2-sided) p-value (1-sided)	0.0000 0.0000 -4.6007 0.0000	
t p-value (2-sided) p-value (1-sided) Assume Unequal Variance: t p-value (2-sided)	0.0000 0.0000 -4.6007 0.0000	
t p-value (2-sided) p-value (1-sided) Assume Unequal Variance: t p-value (2-sided) p-value (1-sided)	0.0000 0.0000 -4.6007 0.0000	

P-values turn red when results are significant!

#### Rules based yellow highlight to aid interpretation!



#### Statistical Tools: One-Way ANOVA & Means Matrix

L 1		<u> </u>	-	<u> </u>				[
One-Way ANOVA & Means Matrix: Overall Satisfaction	v					4.48	4.48	4.48
	2 2							
H0: Mean 1 = Mean 2 = = Mean k						4.28 -	4.28 -	4.28 +
Ha: At least one pair Mean i ≠ Mean j								
					. u 4.08 -			
Customer Type	1	2	3		tistao			
Count	31	42	27		4.08 - 3.68 - 3.68 -			
Mean	3.3935	4.2052	3.6411		Dvera			
Standard Deviation	0.824680	0.621200	0.670478		<u>5</u> 3.68		T	T
UC (2-sided, 95%, pooled)	3.6441	4.4205	3.9096		- 3.08 - Wear			
LC (2-sided, 95%, pooled)	3.1430	3.9900	3.3727		≥ <sub>3.48</sub> -			
							t	
ANOVA:					3.28 -			
Pooled Standard Deviation =	0.702810		R-Sq =	20.95%			l	
DF =	97		R-Sq adj. =	19.32%	3.08		1	. 1
F =	12.856					1		
p-value =	0.0000							
Pairwise Mean Difference (row - column)	1	2	-					
1	0	-0.811690	-0.247563					
2		0	0.564127					
3			0					
Pairwise Probabilities	1	2	3					
1		0.0000	0.1840					
2			0.0016					
3								
1								



### Statistical Tools: One-Way ANOVA & Means Matrix

	One-Way ANOVA Assumpt	ions Report				
Normality:	Anderson Darling P-Value = 0.531. Fail to reject null hypothesis: "data are sampled from a normal distribution," so conclude that the assumption of normality is not violated.	Anderson Darling P-Value = 0.030. Reject null hypothesis: "data are sampled from a normal distribution," so conclude that the assumption of normality is violated (at 95% confidence level). Skewness value = -0.9680 and Kurtosis value = 0.6796. See robustness and outliers.	Anderson Darling P-Value = 0.360. Fail to reject null hypothesis: "data are sampled from a normal distribution," so conclude that the assumption of normality is not violated.			
Robustness:	Minimum sample size for a robust ANOVA test = 2. Since each sample size is greater than this, the ANOVA test is robut to nonnormality.					
Outliers (Boxplot Rules):	No outliers found.	Potential (1.5*IQR) outlier lower count = 1. It is recommended to review the data with graphical tools: Boxplot, Normal Probability Plot, Histogram and Run Chart / Control Chart. Consider using a Nonparametric Test.	No outliers found.			
Randomness (Independence):	Nonparametric Runs Test (Exact) P- Value = 0.066. Fail to reject null hypothesis: "data are random," so conclude that the assumption of randomness (serial independence) is not violated.	Nonparametric Runs Test (Exact) P-Value = 1.000. Fail to reject null hypothesis: "data are random," so conclude that the assumption of randomness (serial independence) is not violated.	Nonparametric Runs Test (Exact) P Value = 1.000. Fail to reject null hypothesis: "data are random," so conclude that the assumption of randomness (serial independence) is not violated.			
Equal Variance:		P-Value = 0.115. Fail to reject null hypothesis: "v ption of equal variances (or standard deviations)				



## Statistical Tools: Correlation Matrix

Pearson Correlations	Avg No. of orders per mo	Avg days Order to delivery time	Loyalty - Likely to Recommend	<b>Overall Satisfaction</b>	<b>Responsive to Calls</b>	Ease of Communications	Staff Knowledge
Avg No. of orders per mo	1 1	-0.0518	-0.0491	0.1155	0.1076	0.0885	0.0186
Avg days Order to delivery time		1	0.1307	0.3210	0.2725	0.2681	-0.0781
Loyalty - Likely to Recommend			1	0.6599	0.5805	0.4622	0.0176
Overall Satisfaction				1	0.8262	0.7454	0.0766
Responsive to Calls		N			1	0.3791	0.0845
Ease of Communications						1	0.0506
Staff Knowledge							1
Pearson Probabilities	Ava No. of orders per mo.	Avg days Order to delivery time	l ovalty - Likely to Recommend	Overall Satisfaction	Responsive to Calls	Fase of Communications	Staff Knowledge
Avg No. of orders per mo	Avg no. or orders per mo	0.6090	0.6279		0.2865		0.8541
Avg days Order to delivery time	0 -	0.0050	0.1949		0.0061	0.0070	0.4398
Loyalty - Likely to Recommend		a0	0.1343	0.0000	0.000	0.0000	0.8622
Overall Satisfaction		10		0.0000	0.0000	0.0000	0.4490
Responsive to Calls					0.0000	0.0001	0.4035
Ease of Communications						0.0001	0.6171
Staff Knowledge							0.0171
otali rtilowiedge							2
Spearman Rank Correlations	Avg No. of orders per mo	Avg days Order to delivery time	Loyalty - Likely to Recommend	<b>Overall Satisfaction</b>	Responsive to Calls	Ease of Communications	Staff Knowledge
Avg No. of orders per mo	1	-0.0305	-0.0917	0.1006	0.0738	0,1000	0.0187
Avg days Order to delivery time		1	0.1097	0.3407	0.2489	0.2613	-0.0828
Loyalty - Likely to Recommend		1.1	1	0.6167	0.5507	0.4071	-0.0190
Overall Satisfaction		80		1	0.7782	0.7509	0.0890
Responsive to Calls		0			1	0.3204	0.0895
Ease of Communications						1	0.0716
Staff Knowledge							1
Spearman Rank Probabilities	Avg No. of orders per mo	Avg days Order to delivery time	Levelty Likely to Decommond	Overall Satisfaction	Deenensive to Calle	Ease of Communications	Staff Knowledge
	Avg No. of orders per mo		Loyalty - Likely to Recommend 0.3643				
Avg No. of orders per mo		0.7629					0.8532
Avg days Order to delivery time			0.2774		0.0125		0.4127
Loyalty - Likely to Recommend		s		0.0000	0.0000	0.0000	0.8514
Overall Satisfaction			5		0.0000	0.0000	0.3786
Responsive to Calls						0.0012	0.3758
Ease of Communications Staff Knowledge							0.4792



## Statistical Tools: Multiple Linear Regression

- Accepts continuous and/or categorical (discrete) predictors.
  - Categorical Predictors are coded with a 0,1 scheme making the interpretation easier than the -1,0,1 scheme used by competitive products.
- Interactive Predicted Response Calculator with 95% Confidence Interval and 95% Prediction Interval.



## Statistical Tools: Multiple Linear Regression

- Residual plots: histogram, normal probability plot, residuals vs. time, residuals vs. predicted and residuals vs. X factors
- Residual types include Regular, Standardized, Studentized
- Cook's Distance (Influence), Leverage and DFITS
- Highlight of significant outliers in residuals
- Durbin-Watson Test for Autocorrelation in Residuals with p-value
- Pure Error and Lack-of-fit report
- Collinearity Variance Inflation Factor (VIF) and Tolerance report
- Fit Intercept is optional



# Statistical Tools: Multiple Regression

Customer Record No Order Date Avg No. of orders per Avg days Order to deli Loyalty - Likely to Recc Staff Knowledge Size of Customer	Numeric Response (Y) >>	Overall Satisfaction	<u>0</u> K >>
			Cancel
	Continuous <u>P</u> redictors (X) >>	Responsive to Calls Ease of Communication	Help
Major-Complaint Product Type Sat-Discrete	(Numeric Data)		
	Categorical Predictors (X) >>	Customer Type	
	(Text or Numeric Discrete Data)		
	<< <u>R</u> emove	🔽 Fit Intercept	
		☑ Display Residual Plots	

Multiple Regression accepts Continuous and/or Categorical Predictors!



# Statistical Tools: Multiple Regression

Multiple Regression Model: Overall Satisfaction = (0.552345) + (0.427400) \* Responsive to Calls + (0.409625) \* Ease of Communications + (0.132728) \* Customer Type\_2 + (0.023142) \* Customer Type\_3

#### Model Summary:

R-Square	90.58%
R-Square Adjusted	90.18%
S (Root Mean Square Error)	0.245199119

#### Parameter Estimates:

Predictor Term	Coefficient	SE Coefficient	Т	Р	VIF	Tolerance
Constant	0.552345	0.120148	4.5972	0.0000		
Responsive to Calls	0.427400	0.023788018	17.967	0.0000	1.2116	0.825379
Ease of Communications	0.409625	0.031120872	13.162	0.0000	1.3246	0.754950
Customer Type_2	0.132728	0.063914154	2.0767	0.0405	1.6551	0.604180
Customer Type_3	0.023141785	0.065217411	0.354841	0.7235	1.3944	0.717173

#### Analysis of Variance for Categorical (Discrete) Predictors:

Predictor Term	DF	SS	MS	F	Р
Customer Type	2	0.299651	0.149825574	2.492000584	0.0881

#### Analysis of Variance for Model:

Source	DF	SS	MS	F	Р
Model	4	54.901	13.725	228.29	0.0000
Error	95	5.7116	0.060122608		
Total (Model + Error)	99	60.612	0.612246		[ ]

Durbin-Watson Test for Autocorrelation in Residuals:		$\frown$
DW Statistic	X	1.7302
P-Value Positive Autocorrelation	(	0.0888
P-Value Negative Autocorrelation		0.9137

Durbin-Watson Test with p-values for positive and negative autocorrelation!



#### Statistical Tools: Multiple Regression – Predicted Response Calculator with Confidence Intervals

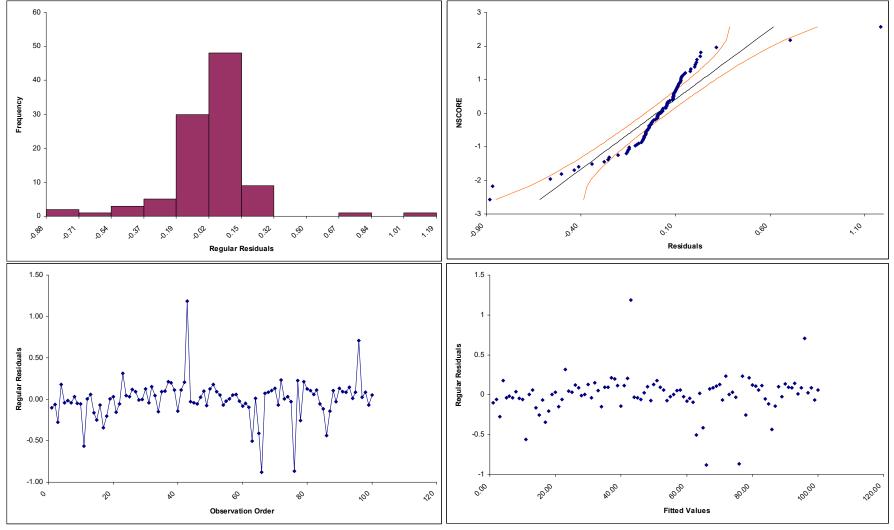
Predicted Response Calculator:

Predictors	Enter Settings:	Predicted Response	Lower 95% Cl	Upper 95% Cl	Lower 95% Pl	Upper 95% PI
Responsive to Calls	5	0.99238657	4.778492731	4.961905131	4.374854056	5.365543806
Ease of Communications	5					20 20
Customer Type_2	1					
Customer Type_3	0					

#### Easy-to-use Calculator with Confidence Intervals and Prediction Intervals!



#### Statistical Tools: Multiple Regression with Residual Plots





### Statistical Tools: Binary and Ordinal Logistic Regression

- Powerful and user-friendly logistic regression.
- Report includes a calculator to predict the response event probability for a given set of input X values.
- Categorical (discrete) predictors can be included in the model in addition to continuous predictors.
- Model summary and goodness of fit tests including Likelihood Ratio Chi-Square, Pseudo R-Square, Pearson Residuals Chi-Square, Deviance Residuals Chi-Square, Observed and Predicted Outcomes – Percent Correctly Predicted.



### Statistical Tools: Nonparametric Tests

- 1 Sample Sign
- 1 Sample Wilcoxon
- 2 Sample Mann-Whitney
- Kruskal-Wallis Median Test
- Mood's Median Test
- Kruskal-Wallis and Mood's include a graph of Group Medians and 95% Median Confidence Intervals
- Runs Test



### Statistical Tools: Nonparametric Tests - Exact

- 1 Sample Wilcoxon Exact
- 2 Sample Mann-Whitney Exact & Monte Carlo Exact
- Kruskal-Wallis Exact & Monte Carlo Exact
- Mood's Median Test Exact & Monte Carlo Exact
- Runs Test Exact



### Statistical Tools: Chi-Square Test

Chi-Square Test			
Major-Complaint - Customer Type			0
Observed Counts	1	2	
Difficult-to-order	5	9	
Not-available	2	0	1
Order-takes-too-long	1	3	(
Return-calls	19	28	1:
Wrong-color	4	2	
Expected Counts	1	2	
Difficult-to-order	5.8900	7.9800	5.130
Not-available	1.2400	1.6800	1.08
Order-takes-too-long	3.1000	4.2000	2.700
Return-calls	18.600	25.200	16.20
Wrong-color	2.1700	2.9400	1.8900
Std. Residuals	1	2	
Difficult-to-order	-0.366718	0.361076	-0.057396402
Not-available	0.682500	-1.2961	0.88527
Order-takes-too-long	-1.1927	-0.585540	2.008
Return-calls	0.092747779	0.557773	-0.79504
Wrong-color	1.2423	-0.548219	-0.64738
Chi-Square	12.211		8
DF	8		
p-value	0.1420		9
Note: 9 out of 15 cells have expected counts less than 5.			



### Statistical Tools: Chi-Square Test – Fisher's Exact

Chi-Square - Fisher's Exact			
Major-Complaint - Customer	Туре		
Observed Counts	1	2	3
Difficult-to-order	5	9	1
Not-available	2	0	2
Order-takes-too-long	1	3	(
Return-calls	19	28	1:
Wrong-color	4	2	
Expected Counts	1	2	:
Difficult-to-order	5.890	7.980	5.13
Not-available	1.240	1.680	1.0
Order-takes-too-long	3.100	4.200	2.70
Return-calls	18.600	25.200	16.20
Wrong-color	2.170	2.940	1.89
Std. Residuals	1	2	:
Difficult-to-order	-0.366718	0.361076	-0.057396402
Not-available	0.682500	-1.296	0.88527
Order-takes-too-long	-1.193	-0.585540	2.00
Return-calls	0.092747779	0.557773	-0.79504
Wrong-color	1.242	-0.548219	-0.64738
Chi-Square	12.211		
DF	8		
Chi-Square P-Value	0.1420		
Fisher's Exact P-Value	0.1469	>	



### Statistical Tools: Chi-Square Test – Fisher's Monte Carlo

Chi-Square Test - Fisher's Monte-Carlo			
Major-Complaint - Customer Type			
Observed Counts	1	2	3
Difficult-to-order	5	9	3 5 2
Not-available	2	0	2
Order-takes-too-long	1	3	6
Return-calls	19	28	13
Wrong-color	4	2	1
Expected Counts	1	2	3
Difficult-to-order	5.890	7.980	5.130
Not-available	1.240	1.680	1.08
Order-takes-too-long	3.100	4.200	2.700
Return-calls	18.600	25.200	16.200
Wrong-color	2.170	2.940	1.890
Std. Residuals	1	2	3
Difficult-to-order	-0.366718	0.361076	-0.057396402
Not-available	0.682500	-1.296	0.885270
Order-takes-too-long	-1.193	-0.585540	2.008
Return-calls	0.092747779	0.557773	-0.795046
Wrong-color	1.242	-0.548219	-0.647380
Chi-Square	12.211		
DF	8		
Chi-Square P-Value	0.1420		
Fisher's Monte-Carlo P-Value	0.1486	>	
Fisher's Monte-Carlo P-Value 99% CI Upper	0.1569		
Fisher's Monte-Carlo P-Value 99% CI Lower	0.1403		

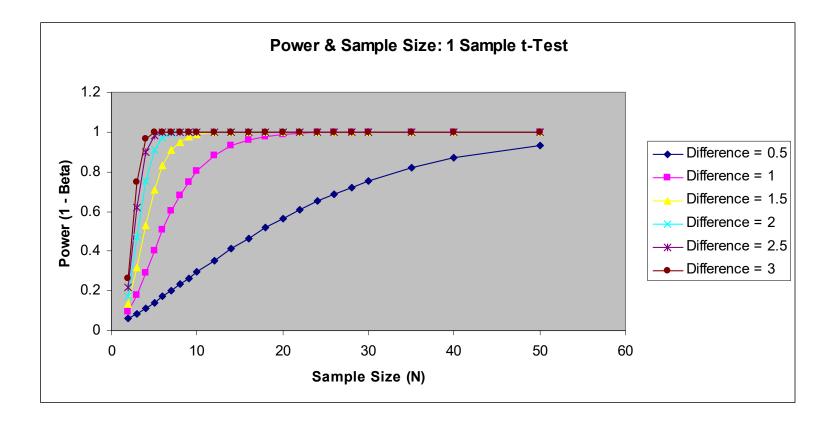


# Statistical Tools: Power & Sample Size Calculators

- 1 Sample t-Test
- 2 Sample t-Test
- One-Way ANOVA
- 1 Proportion Test
- 2 Proportions Test
- The Power and Sample Size Calculators allow you to solve for Power (1 – Beta), Sample Size, or Difference (specify two, solve for the third).



# Statistical Tools: Power & Sample Size Charts





### Measurement Systems Analysis

- Basic MSA Templates
- Create Gage R&R (Crossed) Worksheet
  - Generate worksheet with user specified number of parts, operators, replicates
- Analyze Gage R&R (Crossed)
- Attribute MSA (Binary)
- Attribute MSA (Ordinal)
- Attribute MSA (Nominal)



#### Measurement Systems Analysis: Gage R&R Template

Gage Name: Date of Study: Performed By:	20-May-04 John Noguera	Gage R&R Metrics	StDev	StDev * Multiplier	% Total Variation (TV)	% Tolerance
Notes:		Gage R&R:	0.000854184	0.004399046	11.46	22.00
		Operator (AV Appraiser Variation):	0	0	0.00	0.00
Process Tolerance		Operator * Part (INT Interaction):	0.0005288	0.002723321	7.09	13.62
USL:	0.05	Reproducibility (SQRT(AV^2 + INT^2)):	0.0005288	0.002723321	7.09	13.62
LSL:	0.03	Repeatability (EV Equipment Variation):	0.00067082	0.003454725	9.00	17.27
StDev Multiplier:	5.15	Part Variation (PV):	0.007405954	0.038140661	99.34	190.70
		Total Variation (TV):	0.00745505	0.03839351	100.00	191.97

Operator A	Part 1	Part 2	Part 3
Reading 1	0.03	0.035	0.041
Reading 2	0.031	0.034	0.042
Reading 3	0.032	0.036	0.042

Operator B	Part 1	Part 2	Part 3
Reading 1	0.031	0.035	0.042
Reading 2	0.031	0.034	0.041
Reading 3	0.032	0.035	0.04

Operator C	Part 1	Part 2	Part 3
Reading 1	0.032	0.034	0.043
Reading 2	0.032	0.034	0.041
Reading 3	0.032	0.033	0.042



#### Measurement Systems Analysis: Create Gage R&R (Crossed) Worksheet

Number of Parts	s/Samples:	10	-	<u>0</u> K>>
Number of Oper	ators/Appraisers:	3		Cance
Number of Repl	cates/Trials:	3	•	Help
	Randomize Parts/	Samples		Rese
1	Randomize Operal	ors/App	raisers	
Part/Sample Na	mes:			
1:	Part 1		-	
2:	Part 2			
3:	Part 3			
	Daet 4			
Operator/Appra	iser Names::			
1:	Operator A			
2:	Operator B			
	Operator C			

Gage R&R Study (Crossed) Worksheet

Gage Name:	Calipers
Date of Study:	26-Apr-06
Performed By:	John Noguera
Notes:	

Run Order	Std. Order	Parts	Operators	Measurement
1	12	Part 4	Operator A	0.676
2	2	Part 1	Operator A	0.898
3	20	Part 7	Operator A	0.398
4	24	Part 8	Operator A	0.948
5	17	Part 6	Operator A	0.932
6	6	Part 2	Operator A	0.934
7	27	Part 9	Operator A	0.689
8	15	Part 5	Operator A	0.538
9	29	Part 10	Operator A	0.704



Measurement Systems Analysis: Analyze Gage R&R (Crossed)

- ANOVA, %Total, %Tolerance (2-Sided or 1-Sided), %Process, Variance Components, Number of Distinct Categories
- Gage R&R Multi-Vari and X-bar R Charts
- Confidence Intervals on %Total, %Tolerance, %Process and Standard Deviations
- Handles unbalanced data (confidence intervals not reported in this case)



#### Measurement Systems Analysis: Analyze Gage R&R (Crossed)

Analyze Gage R&R (Cros	sed)		
Run Order Std. Order	<u>P</u> art >>	Parts	<u>0</u> K>>
	Op <u>e</u> rator >>	Operators	Cancel
	Measurement >>	Measurement	Help
	<< <u>R</u> emove		
✓ Display Multi-Yari & X	-Bar R Charts	Standard Deviation Multiplier: Alpha to Remove Interaction: Confidence Level:	6 <b>•</b> 0.1 90 %
<b>Report</b> <u>I</u> nformation (	Optional)	✓ <u>I</u> olerance/Historical StDev	(Optional)
Gage Name: Performed By: Date: Notes:		Upper-Lower Spec:     1     Upper Spec:     Lower Spec:     Historical Process     Standard Deviation:	



#### Measurement Systems Analysis: Analyze Gage R&R with Confidence Intervals

Analysis of Variance with Part ^ Operator Interaction:							
Source	DF	SS	MS	F	Р		
Part:	9	0.553693	0.061521481	37.103	0.0000		
Operator:	2	0.013653333	0.006826667	4.1170	0.0337		
Part * Operator:	18	0.029846667	0.001658148	4.1111	0.0003		
Repeatability:	30	0.0121	4.033E-04				
Total:	59	0.609293	0.010327006				

		StDev	StDev		% Total	% TV	% TV
Gage R&R Metrics	StDev	Lower 90% Cl	Upper 90% Cl	6 * StDev	Variation (TV)	Lower 90% Cl	Upper 90% Cl
Gage R&R:	0.035904967	0.030367917	0.087410367	0.215430	33.83	20.16	68.36
Operator (AV Appraiser Variation):	0.016075631	0.004168708	0.081026508	0.096453789	15.15		
Part * Operator (INT Interaction):	0.025048102	0.017095374	0.037247076	0.150289	23.60		
Reproducibility (SQRT(AV^2 + INT^2)):	0.029762952	0.021365632	0.085000016	0.178578	28.04		
Repeatability (EV Equipment Variation):	0.02008316	0.016626072	0.025579555	0.120499	18.92		
Part Variation (PV):	0.099886046	0.071946598	0.165736	0.599316	94.10		
Total Variation (TV):	0.106143247	0.080362383	0.172845	0.636859	100.00		

**Confidence Intervals are calculated for Gage R&R Metrics!** 



#### Measurement Systems Analysis: Analyze Gage R&R with Confidence Intervals

Gage R&R Metrics	% Tolerance	% Tolerance Lower 90% Cl	% Tolerance Upper 90% Cl
Gage R&R:	21.54	18.22	52.45
Operator (AV Appraiser Variation):	9.65	2.50	48.62
Part * Operator (INT Interaction):	15.03	10.26	22.35
Reproducibility (SQRT(AV^2 + INT^2)):	17.86	12.82	51.00
Repeatability (EV Equipment Variation):	12.05	9.98	15.35
Part Variation (PV):	59.93	43.17	99.44
Total Variation (TV):	63.69	48.22	103.71

Gage R&R Metrics	Variance Component	% Contribution of Variance Component
Gage R&R:	0.001289167	11.44
Operator:	2.584E-04	2.29
Part * Operator:	6.274E-04	5.57
Reproducibility:	8.858E-04	7.86
Repeatability:	4.033E-04	3.58
Part Variation:	0.009977222	88.56
Total Variation:	0.011266389	100.00

Gage R&R Metrics	NDC	NDC Lower 90% Cl	NDC Upper 90% Cl
Number of Distinct Categories			
(Signal-to-Noise Ratio: 1.41 * PV/R&R):	3.9	1.5	6.9

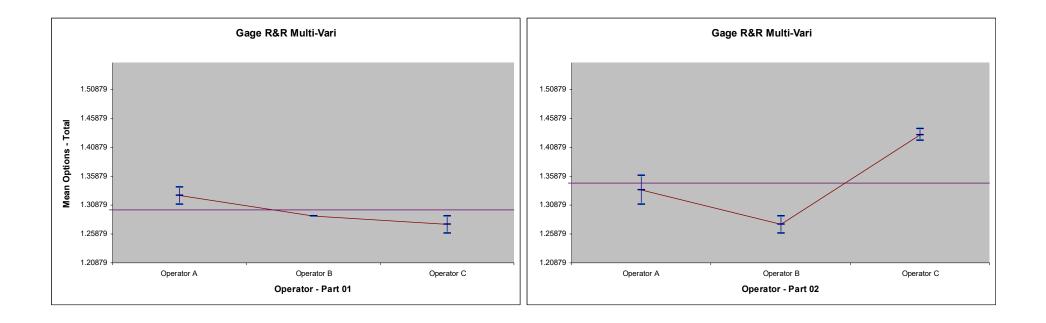


#### Measurement Systems Analysis: Analyze Gage R&R – X-bar & R Charts





#### Measurement Systems Analysis: Analyze Gage R&R – Multi-Vari Charts





Measurement Systems Analysis: Attribute MSA (Binary)

- Any number of samples, appraisers and replicates
- Within Appraiser Agreement, Each Appraiser vs Standard Agreement, Each Appraiser vs Standard Disagreement, Between Appraiser Agreement, All Appraisers vs Standard Agreement
- Fleiss' kappa



#### Attribute Measurement Systems Analysis

- "Traffic Light" Attribute Measurement Systems Analysis: Binary, Ordinal and Nominal
  - ✓ A Kappa color highlight is used to aid interpretation: Green (> .9), Yellow (.7-.9) and Red (< .7) for Binary and Nominal.</p>
  - ✓ Kendall coefficients are highlighted for Ordinal.
  - ✓ A new Effectiveness Report treats each appraisal trial as an opportunity, rather than requiring agreement across all trials.

Each Appraiser vs. Standard Agreement	# Inspected	# Matched	Percent	95.0% LC (Exact)	95.0% UC (Exact)	Fleiss' Kappa	Fleiss' Kappa P-Value	Fleiss' Kappa 95.0% LC	Fleiss' Kappa 95.0% UC
Α	50	42	84.00	70.89	92.83	0.8802	0.0000	0.7202	1.0000
В	50	45	90.00	78.19	96.67	0.9226	0.0000	0.7626	1.0000
С	50	40	80.00	66.28	89.97	0.7747	0.0000	0.6147	0.9347

Each Appraiser vs. Standard Agreement	# Inspected	# Matched	Percent	95.0% LC (Score)	95.0% UC (Score)	Kendall's Correlation Coeff.	Kendall's Correlation P-Value	Kendall's Correlation 95.0% LC	Kendall's Correlation 95.0% UC
Joe	50	11	22.00	12.75	35.24	0.7323	0.0000	0.6218	0.8427
Мое	50	2	4.00	1.10	13.46	0.4161	0.0000	0.3057	0.5265
Sue	50	40	80.00	66.96	88.76	0.9495	0.0000	0.8391	1.0000

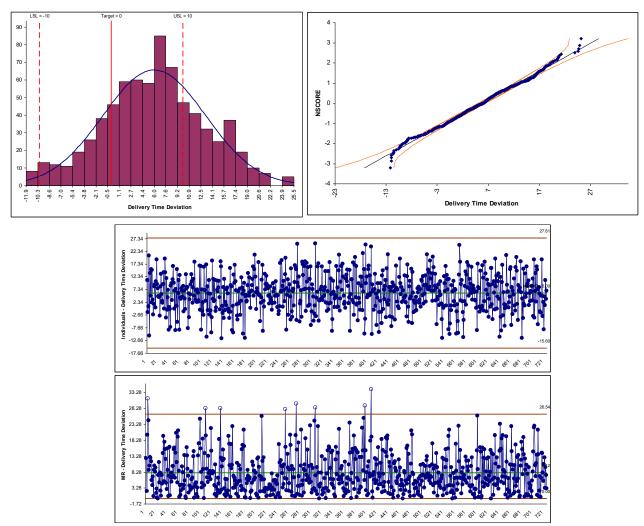


### **Process Capability** (Normal Data)

- Process Capability/Sigma Level Templates
- Multiple Histograms and Process Capability
- Capability Combination Report for Individuals/Subgroups:
  - Histogram
  - Capability Report (Cp, Cpk, Pp, Ppk, Cpm, ppm, %)
  - Normal Probability Plot
  - Anderson-Darling Normality Test
  - Control Charts



#### Process Capability: Capability Combination Report



Count =	725
Mean =	6.0036
StDev (Overall, Long Term) =	7.1616
StDev (Within, Short Term) =	7.2020
USL =	10
Target =	0
LSL =	-10
Constanting Constant Constant	
Capability Indices using Overall StDev	0.47
Pp =	0.47
Ppu =	0.19
Ppl =	0.74
Ppk =	0.19
Cpm =	0.36
Potential Capability Indices using Within StDev	-
Cp =	0.46
	0.46
Cpu =	
Cpl =	0.74
Cpk =	0.18
xpected Overall Performance	
ppm > USL =	288409
ppm < LSL =	12720
ppm Total =	301130
% > USL =	28.84%
% < LSL =	1.27%
% Total =	30.11%
Asteral (Evenisian) Destances	
Actual (Empirical) Performance % > USL =	26.90%
% > 03L =	1.38%
% < LSL = % Total =	28.28%
% Total =	20.20%
Anderson-Darling Normality Test	
Anderson-Darling Normality Test A-Squared =	0.708616



### **Process Capability for Nonnormal Data**

- Box-Cox Transformation (includes an automatic threshold option so that data with negative values can be transformed)
- Johnson Transformation
- Distributions supported:
  - Half-Normal
  - Lognormal (2 & 3 parameter)
  - Exponential (1 & 2 parameter)
  - Weibull (2 & 3 parameter)
  - Beta (2 & 4 parameter)
  - Gamma (2 & 3 parameter)
  - Logistic
  - Loglogistic (2 & 3 parameter)
  - Largest Extreme Value
  - Smallest Extreme Value

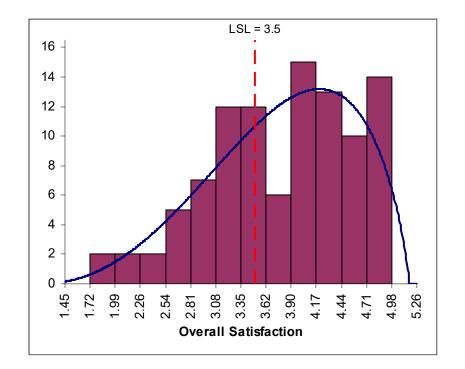


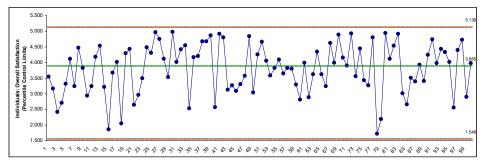
#### **Process Capability for Nonnormal Data**

- Automatic Best Fit based on AD p-value
- Nonnormal Process Capability Indices:
  - Z-Score (Cp, Cpk, Pp, Ppk)
  - Percentile (ISO) Method (Pp, Ppk)
- Distribution Fitting Report
  - All valid distributions and transformations reported with histograms, curve fit and probability plots
  - Sorted by AD p-value



#### Nonnormal Process Capability: Automatic Best Fit





Process Capability Report (Nonnormal): Overall Satisfaction					
Distribution: Beta with Lower/Upper Threshold (4 p)					
Sample Count	100				
Sample Mean	3.801				
Shape1	3.465				
Shape2	1.775				
Upper Threshold (Optimal)	5.170				
Lower Threshold (Optimal)	1.117				
Percentile (Overall Satisfaction)	1				
StDev (Normalized Within, Short Term)	0.949670				
USL					
Target					
LSL	3.5				

Capability Indices (Z-Score Method	
Pp	
Ppu	
Ppl	0.143006
Ppk	0.143006

Potential Capability Indices using Normalized Within StDev						
Ср						
Сри						
Cpl	0.150585					
Cpk	0.150585					

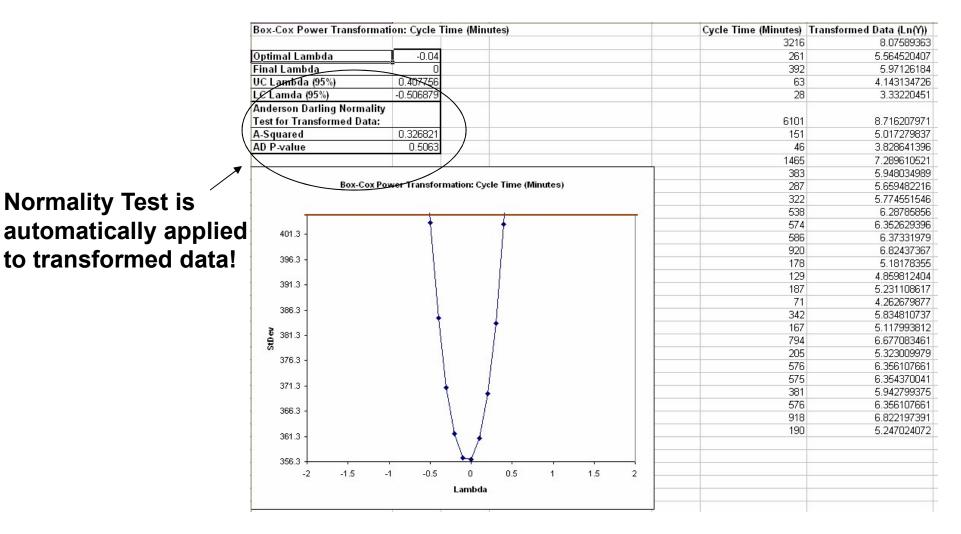
Expected Overall Performance					
ppm > USL					
ppm < LSL	333955				
ppm Total	333955				
% > USL					
% < LSL	0.333955				
% Total	33.40%				

Actual (Empirical) Performance				
% > USL	Ş			
% < LSL	33.00%			
% Total	33.00%			

Anderson-Darling Goodness-of-Fit Tests				
AD Beta (4P)	0.199268			
AD Beta (4P) p-value	0.882 (Z-Score Est.)			
AD Normality Original Data	0.803438292			
AD Normality P-Value Original Data	0.0363			



#### Process Capability: Box-Cox Power Transformation





## Reliability/Weibull Analysis

- Weibull Analysis
  - Complete and Right Censored data
  - Least Squares and Maximum Likelihood methods
  - Output includes percentiles with confidence intervals, survival probabilities, and Weibull probability plot.



## **Design of Experiments**

#### Basic DOE Templates

- Automatic update to Pareto of Coefficients
- Easy to use, ideal for training
- Generate 2-Level Factorial and Plackett-Burman Screening Designs
- Main Effects & Interaction Plots
- Analyze 2-Level Factorial and Plackett-Burman Screening Designs



#### **Basic DOE Templates**

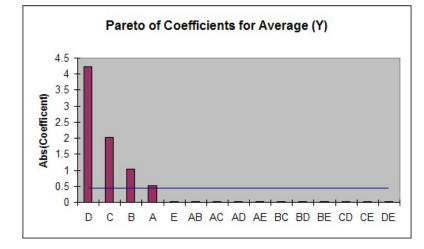
#### Five Factor, Two-Level, Half-Fraction Design of Experiments

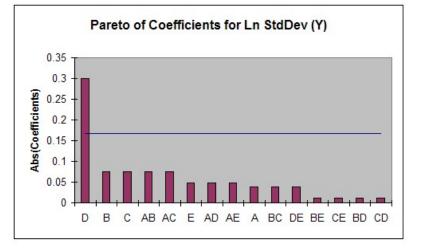
Title: Process Yield Improvement Date: 21-May-04 Name of Experimenter: John Noguera Response: Yield Goal: Maximize

Factor	Factor Name	Low	High
A	Temperature	100	200
в	Power	50	100
С	Pressure	10	20
D	Speed	400	500
E	Catalyst	-1	1

#### Predicted Output for Y:

Factor Name	Enter Actual Factor Setting - uncoded	Factor setting coded		Y-hat:	S-hat:
Tempera	150		0	9.25	1
Power	75		0		
Pressur	15	14 1	0		
Speed	450	5	0		
Catalys	1	1	1		





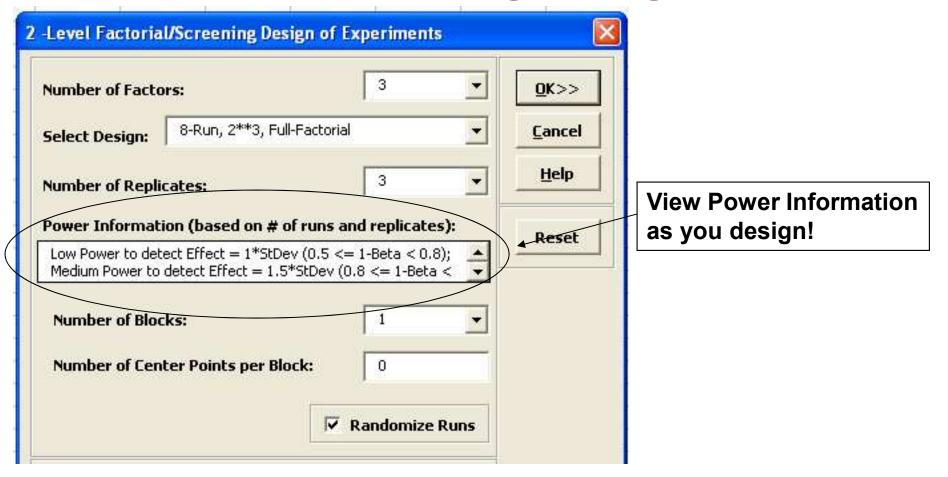


Design of Experiments: Generate 2-Level Factorial and Plackett-Burman Screening Designs

- User-friendly dialog box
- 2 to 19 Factors
- 4,8,12,16,20 Runs
- Unique "view power analysis as you design"
- Randomization, Replication, Blocking and Center Points



#### Design of Experiments: Generate 2-Level Factorial and Plackett-Burman Screening Designs





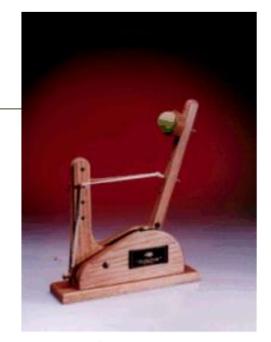
#### Design of Experiments Example: 3-Factor, 2-Level Full-Factorial Catapult DOE

#### **Objective: Hit a target at exactly 100 inches!**

Design of Experiments Worksheet

Title: Catapult Date: April 26 2006 Name of Experimenter: John Noguera Notes:

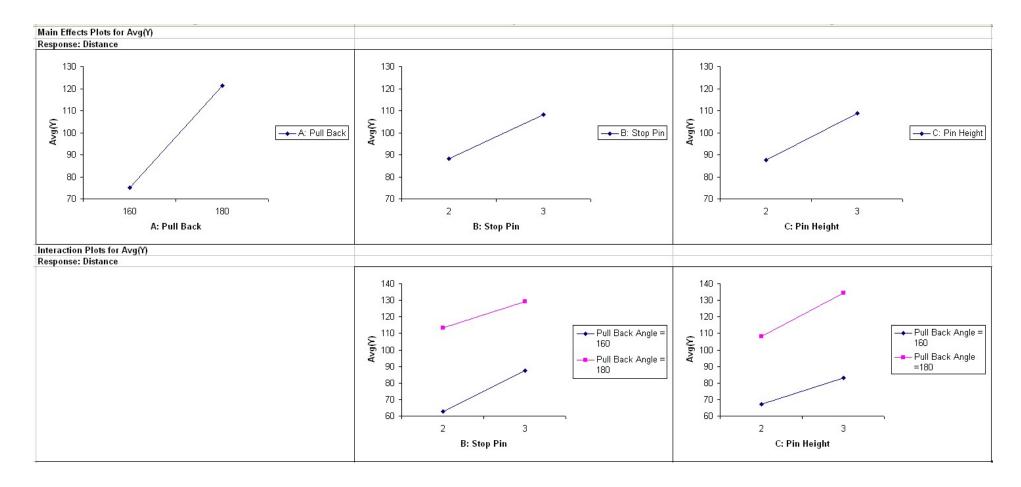
Design Type: 3 Factor, 8-Run, 2\*\*3, Full-Factorial Number of Replicates: 3 Number of Blocks: 1 Number of Center Points per Block: 0 Number of Responses: 1



Run Order	Std. Order	<b>Center Points</b>	Blocks	A: Pull Back	B: Stop Pin	C: Pin Height	Distance
1	11	1	1	160	3	2	80
2	21	1	1	160	2	3	71
3	14	1	1	180	2	3	124
4	19	1	1	160	3	2	79
5	10	1	1	180	2	2	101
6	8	1	1	180	3	3	144
7	2	1	1	180	2	2	102
8	12	1	1	180	3	2	116



#### Design of Experiments: Main Effects and Interaction Plots





Design of Experiments: Analyze 2-Level Factorial and Plackett-Burman Screening Designs

- Used in conjunction with Recall Last Dialog, it is very easy to iteratively remove terms from the model
- Interactive Predicted Response Calculator with 95% Confidence Interval and 95% Prediction Interval.
- ANOVA report for Blocks, Pure Error, Lack-offit and Curvature
- Collinearity Variance Inflation Factor (VIF) and Tolerance report



Design of Experiments: Analyze 2-Level Factorial and Plackett-Burman Screening Designs

- Residual plots: histogram, normal probability plot, residuals vs. time, residuals vs. predicted and residuals vs. X factors
- Residual types include Regular, Standardized, Studentized (Deleted t) and Cook's Distance (Influence), Leverage and DFITS
- Highlight of significant outliers in residuals
- Durbin-Watson Test for Autocorrelation in Residuals with p-value



#### Design of Experiments Example: Analyze Catapult DOE

DOE Multiple Regression Model: Distance = (98.20833333) + (23.125) \* A: Pull Back + (10.125) \* B: Stop Pin + (10.54166667) \* C: Pin Height + (-2.125) \* AB + (2.458333333) \* AC + (0.625) \* BC + (0.708333333) \* ABC

#### Model Summary:

R-Square	99.95%
R-Square Adjusted	99.93%
S (Root Mean Square Error)	0.763763

#### Parameter Estimates:

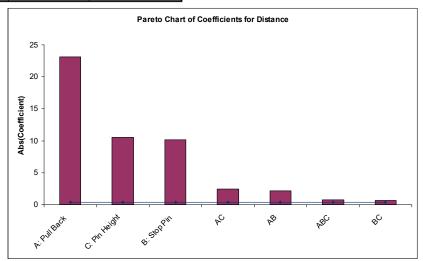
Term	Coefficient	SE Coefficient	Т	Р	VIF	Tolerance
Constant	98.20833333	0.155902391	629.93	0.0000		
A: Pull Back	23.125	0.155902391	148.33	0.0000	1	1
B: Stop Pin	10.125	0.155902391	64.944	0.0000	1	1
C: Pin Height	10.54166667	0.155902391	67.617	0.0000	1	1
AB	-2.125	0.155902391	-13.630	0.0000	1	1
AC	2.458333333	0.155902391	15.768	0.0000	1	1
BC	0.625	0.155902391	4.0089	0.0010	1	1
ABC	0.708333333	0.155902391	4.5434	0.0003	1	1

#### Analysis of Variance for Model:

Source	DF	SS	MS	F	Р
Model	7	18237	2605.2	4466.1	0.0000
Error	16	9.3333	0.583333		
Pure Error	16	9.3333	0.583333		
Total (Model + Error)	23	18246	793.30		

#### Durbin-Watson Test for Autocorrelation in Residuals:

DW Statistic	2.0595
P-Value Positive Autocorrelation	0.5572
P-Value Negative Autocorrelation	0.4357





#### Design of Experiments: Predicted Response Calculator

Predicted Response Calculator:

Predictors	Enter Actual Settings:	Coded Settings	Predicted Response	Lower 95% Cl	Upper 95% Cl	Lower 95% Pl	Upper 95% Pl
A:	179.3	0.93	100.0216667	99.119	100.924	98.168	101.875
B:	2	-1					
C.	2	-1					

Excel's Solver is used with the Predicted Response Calculator to determine optimal X factor settings to hit a target distance of 100 inches. 95% Confidence Interval and Prediction Interval



#### Design of Experiments: Response Surface Designs

• 2 to 5 Factors

runs:

- Central Composite and Box-Behnken Designs
- Easy to use design selection sorted by number of

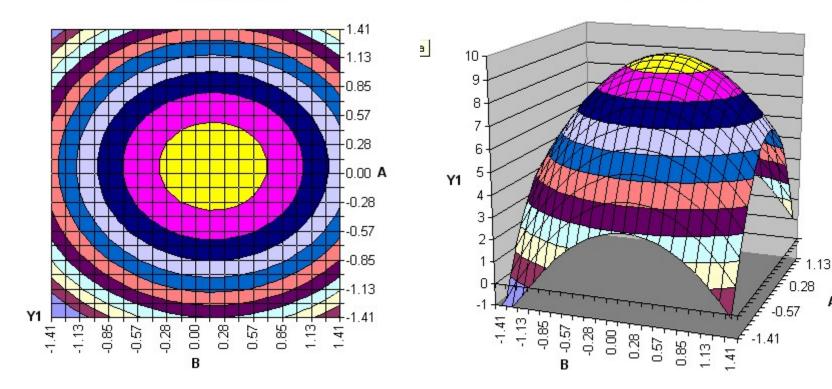
Number of Factor			1	nes and Level Sett				<u>O</u> K>>
Number of Factors	6	2		Name	Low	High	. <u> </u>	Cance
			A:	А	-1	1		
Select Design:	10-Run, Central Com	nposite Design (2 Ctr Pts	В: Г	В	-1	1	-	Help
		1						
Number of Replica	tes:		1					Reset
Block on Repli	ates							
- orders off reepin								
							-	
Alpha Axial Value					-	- 22	_	
Rotatable (Alp	$h_{2} = 1.414$		Number of	Responses:	1	1	_	
anna an air a	ana ana ang ang ang ang ang ang ang ang			Respor	nse Name			
C Face Centered	(Alpha = 1.0)				YI			
	ne: Cube points (	(Circumscribed) 🛛 👻						
Factor Levels Def								



#### Design of Experiments: Contour & 3D Surface Plots

**RSM Multiple Regression Model:** 

Y1 = (9.5) + (0.43) \* A: A + (0.68) \* B: B + (0) \* AB + (-3) \* AA + (-2) \* BB



**RSM** Contour Plot

RSM 3D Surface Plot

А



- Individuals
- Individuals & Moving Range
- X-bar & R
- X-bar & S
- P, NP, C, U
- P' and U' (Laney) to handle overdispersion
- I-MR-R (Between/Within)
- I-MR-S (Between/Within)



- Tests for Special Causes
  - Special causes are also labeled on the control chart data point.
  - Set defaults to apply any or all of Tests 1-8
- Control Chart Selection Tool
  - Simplifies the selection of appropriate control chart based on data type
- Process Capability report
  - Pp, Ppk, Cp, Cpk
  - Available for I, I-MR, X-Bar & R, X-bar & S charts.



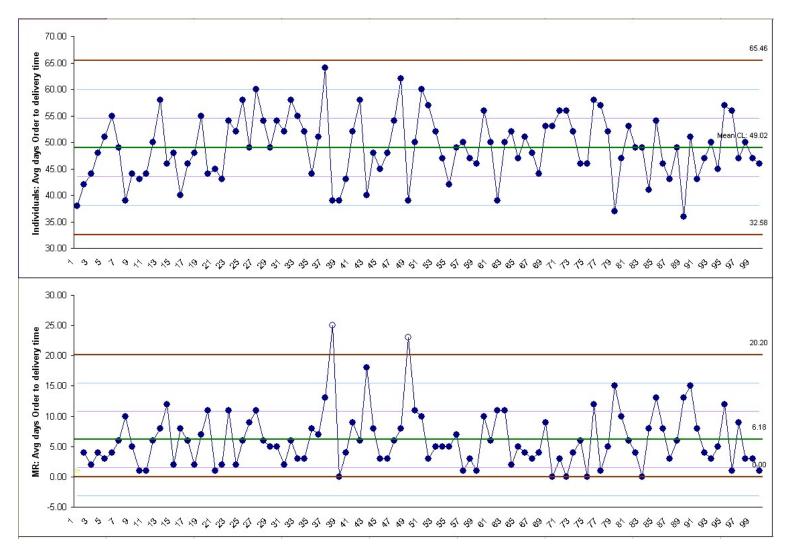
- Add data to existing charts ideal for operator ease of use!
- Scroll through charts with user defined window size
- Advanced Control Limit options: Subgroup Start and End; Historical Groups (e.g. split control limits to demonstrate before and after improvement)



- Exclude data points for control limit calculation
- Add comment to data point for assignable cause
- ± 1, 2 Sigma Zone Lines
- Control Charts for Nonnormal data
  - Box-Cox and Johnson Transformations
  - 16 Nonnormal distributions supported (see Capability Combination Report for Nonnormal Data)
  - Individuals chart of original data with percentile based control limits
  - Individuals/Moving Range chart for normalized data with optional tests for special causes

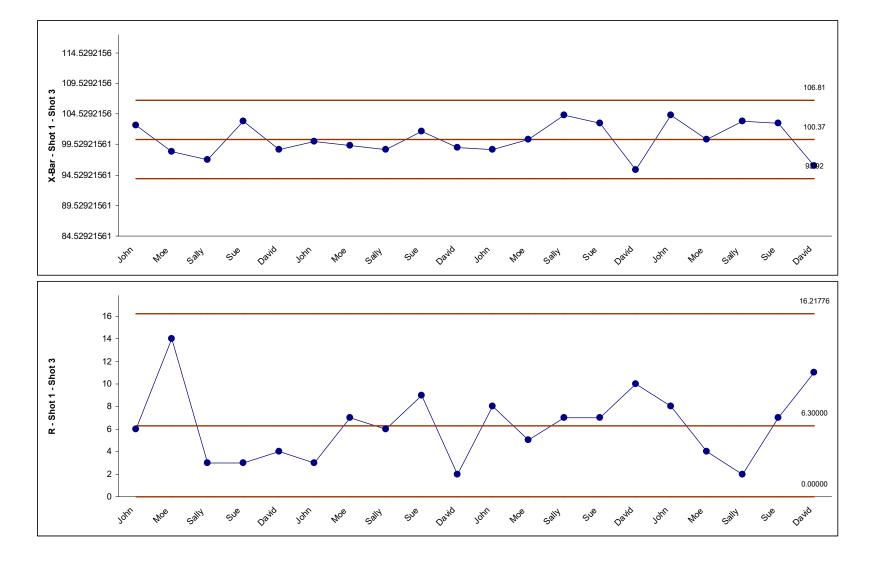


### Control Charts: Individuals & Moving Range Charts



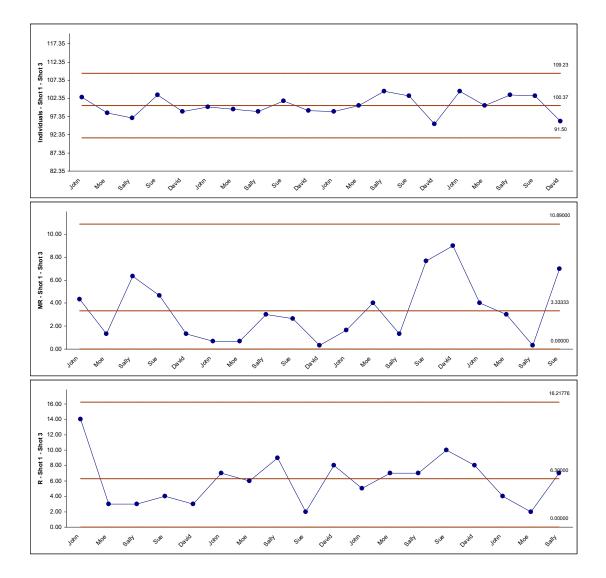


# Control Charts: X-bar & R/S Charts





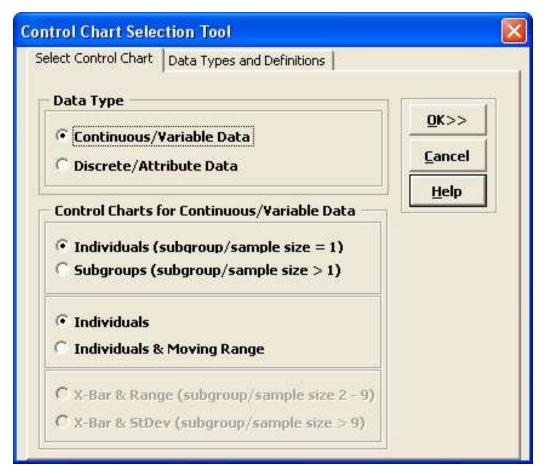
#### Control Charts: I-MR-R/S Charts (Between/Within)





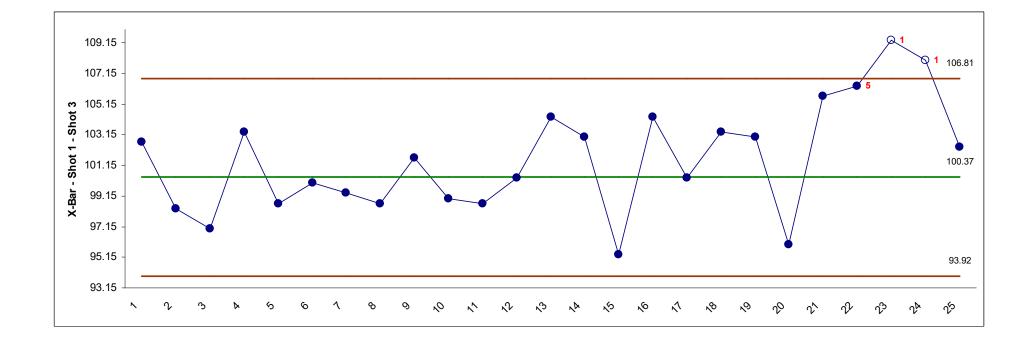
# **Control Chart Selection Tool**

- Simplifies the selection of appropriate control chart based on data type
- Includes Data
   Types and
   Definitions help tab.



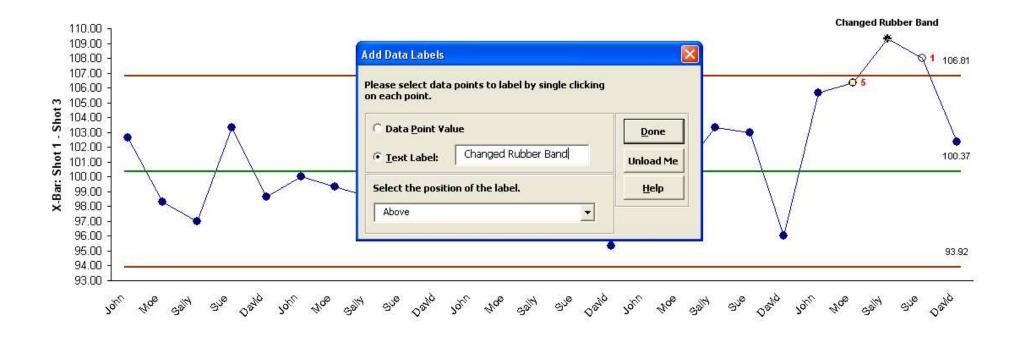


### Control Charts: Use Historical Limits; Flag Special Causes





### **Control Charts: Add Comments as Data Labels**



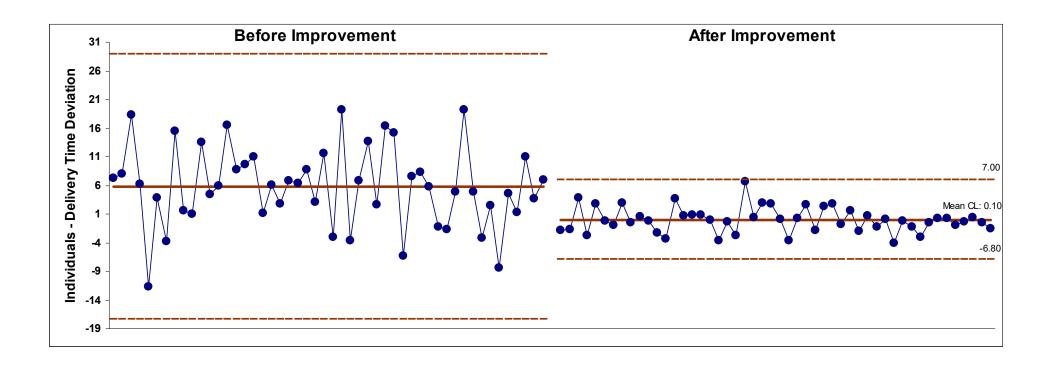


## Control Charts: Summary Report on Tests for Special Causes

Tests for Special Causes - X-Bar - Shot 3 Number of Data Points Failing Tests = 3								
	Test 1: 1 point	Test 2: 9 points	Test 3: 6 points in a row all	Test 4: 14 points	Test 5: 2 out of 3	Test 6: 4 out of 5 points	Test 7: 15 points in a row within 1	Test 8: 8 points in a row more than
Observation No.	more than 3 sigma from CL	in a row on same side of CL	increasing or all decreasing	in a row alternating up and down		more than 1 sigma from CL (same side)	sigma from CL (either side)	1 sigma from CL (either side)
22					X	X		
23	x				x	x		
24	x		9		x	x		

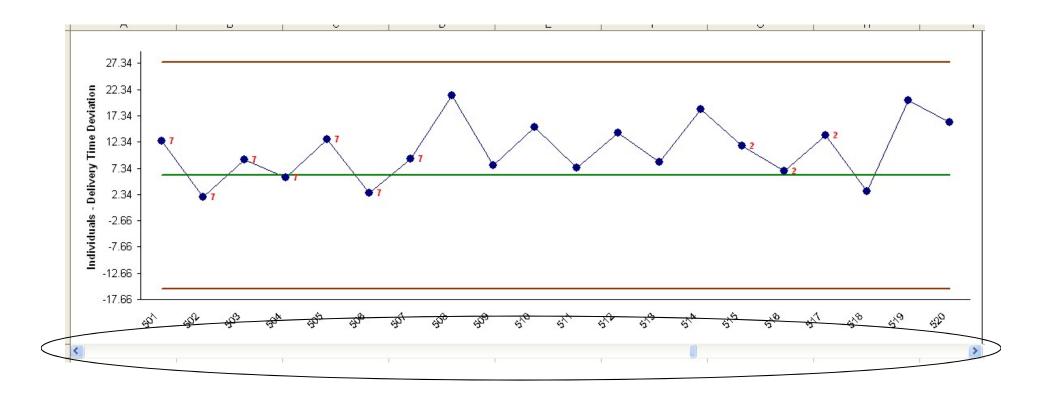


Control Charts: Use Historical Groups to Display Before Versus After Improvement





### Control Charts: Scroll Through Charts With User Defined Window Size



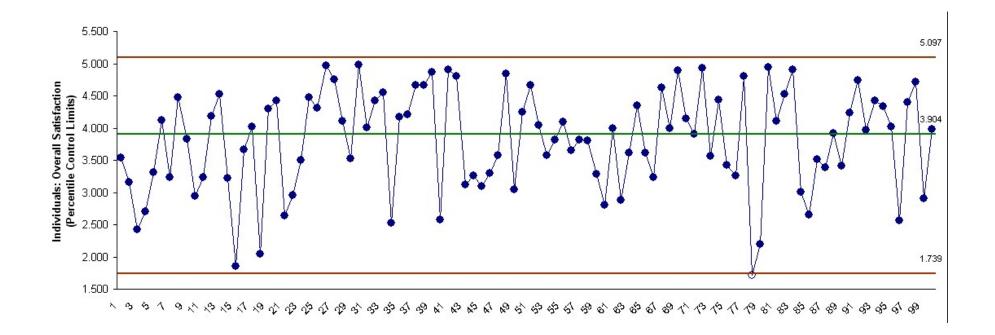


# Control Charts: Process Capability Report (Long Term/Short Term)

Report: X-Bar & R - Shot 1 - Shot 3		
Count =	75	
Mean =	101.56	
StDev (Overall, Long Term) =	4.6156	
StDev (Within, Short Term) =	2.1484	
USL =	108	
Target =	100	
LSL =	92	
Capability Indices using Overall StDev	2	
Pp =	0.58	
Ppu =	0.47	
PpI =	0.69	
Ppk =	0.47	
Cpm =	0.55	
Potential Capability Indices using Within StDev		
Cp =	1.24	
Cpu =	1.00	
Cpl =	1.48	
Cpk =	1.00	
Expected Overall Performance	-	
ppm > USL =	81468	
ppm < LSL =	19168	
ppm Total =	100636	
% > USL =	8.15%	
% < LSL =	1.92%	
% Total =	10.06%	
Actual (Empirical) Performance	5	
% > USL =	5.33%	
% < LSL =	4.00%	
% Total =	9.33%	

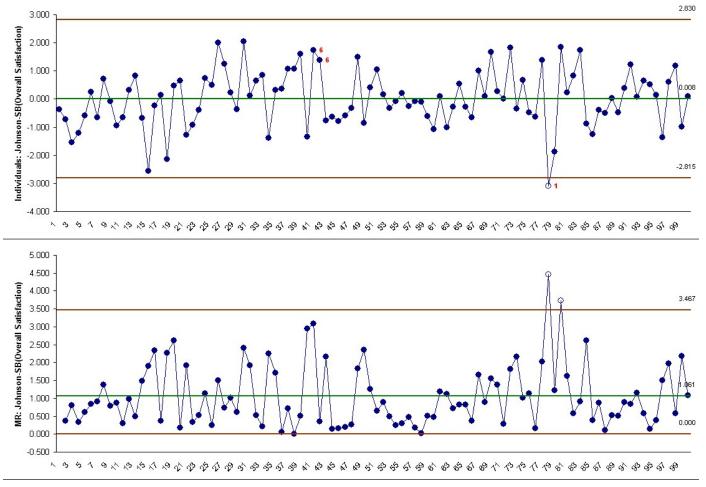


### Individuals Chart for Nonnormal Data: Johnson Transformation





### Individuals/Moving Range Chart for Nonnormal Data: Johnson Transformation



Tests for Special Causes -Number of Data Points Failing Tests = 3



# Control Charts: Box-Cox Power Transformation

